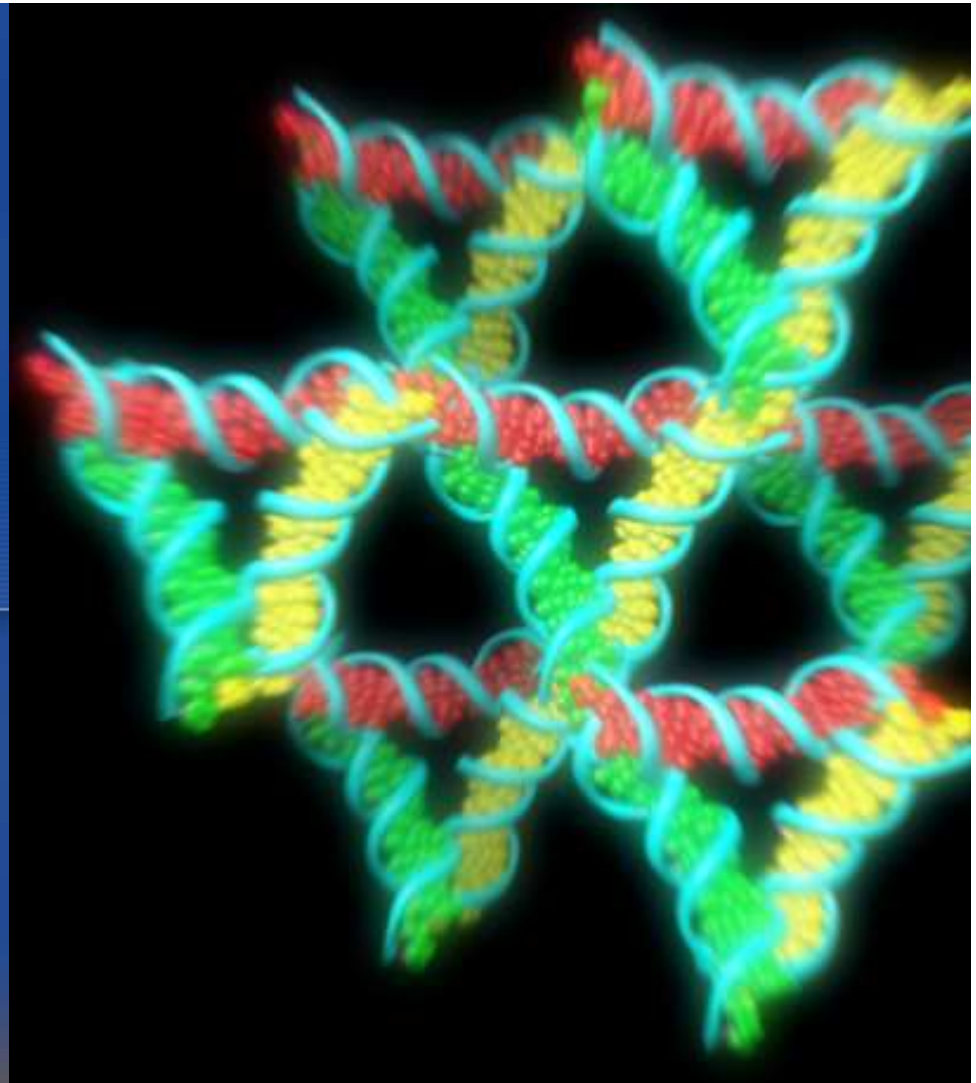


DNA Nanotech

Luca Cardelli

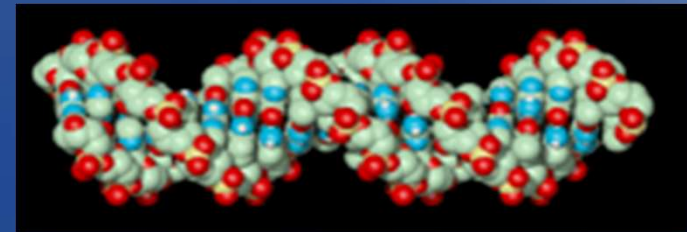
University of Oxford

2021-09-21, Applied Systems Biology
MSc course, Pázmány Péter Catholic University
Budapest (virtual)



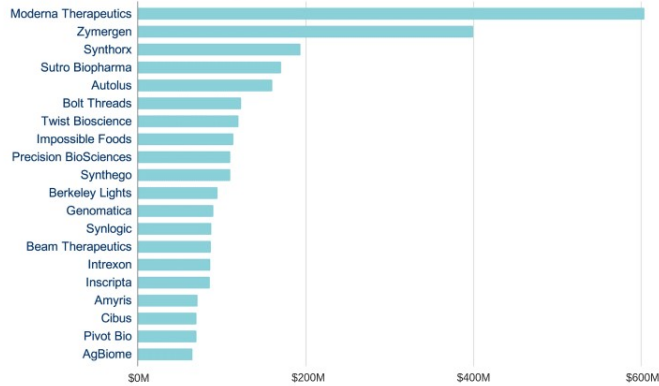
Objectives

- The promises of DNA Nanotechnology:
 - In Science & Medicine
 - In Engineering
 - In Computing
- The current practice of DNA Nanotechnology
 - DNA capabilities
 - Molecular languages and tools
 - Molecular programming



Synthetic Biology Market

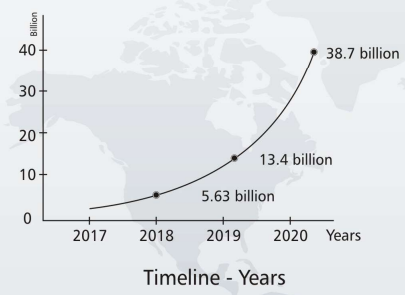
Top synthetic biology fundraisers of 2018 



SYNTHETIC BIOLOGY TECHNOLOGY INNOVATIONS LANDSCAPE



Synthetic Biology Market Size & Growth

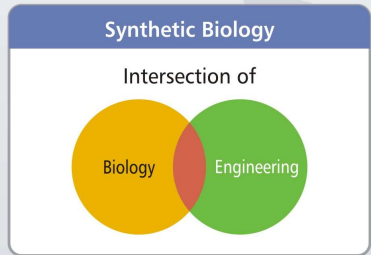


Key Enabling Technologies

- ✓ DNA Synthesis
- ✓ Sequencing Technologies
- ✓ Genome Engineering
- ✓ Microfluidics Technologies
- ✓ Bioinformatics technologies
- ✓ Biological Components & integrated Systems
- ✓ Pathway engineering
- ✓ Biofuels Technologies

Synthetic Biology : Core Market Segments

- DNA Synthesis
- Oligonucleotide Synthesis
- Pharmaceuticals
- Chemicals
- Biofuels
- Agriculture
- Synthetic DNA
- Synthetic Genes
- Synthetic Cells
- XNA
- Chassis organisms
- Enabling Products



For more information, Visit - <https://www.pintels.com> for email : contactus@vajrasoftinc.com

Some (ongoing) successes stories



- (\$4Bn) Reprogram a patient's own blood cells to recognise and destroy specific cancers.
- 90% remission in terminally ill leukemia patients



- (\$300M) Reprogram yeast to produce fine chemicals
- Antimalarial (in partnership with Sanofi)
- Jet fuel (in partnership with Total)

Molecular "hacking"



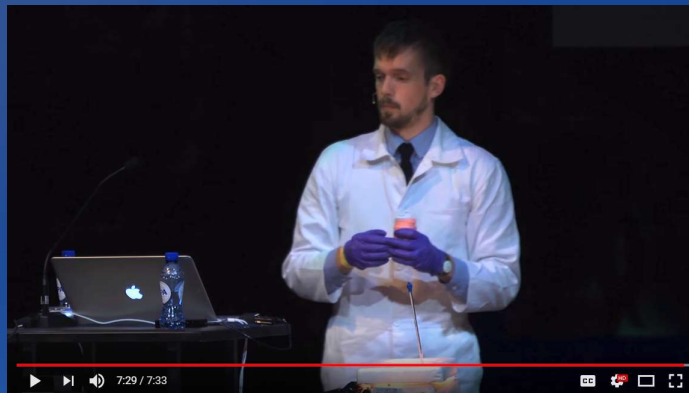
- Supply custom organisms for bio fabrication



- Grow meat, leather (\$100Bn market) in the lab
- Proofs of concept already in production

Hacking Yoghurt

Tuur van Balen - Hacking Yoghurt
- genetically modify your yoghurt in your own kitchen



<https://www.youtube.com/watch?v=Co8NOnErrPU>

Live Clothing

Scientists Sew Genetically Modified E. Coli into Living Clothing



Harnessing the hygroscopic and biofluorescent behaviors of genetically tractable microbial cells to design biohybrid wearables

Wen Wang^{1,2}, Lining Yao², Chin-Yi Cheng^{2,3}, Teng Zhang⁴, Hiroshi Atsumi⁵, Luda Wang⁴, Guanyun Wang², Oksana Anilionyte...

✦ See all authors and affiliations

Molecular Programming

A technology (and theory of computation)
based on information-bearing molecules
of historically biological origin (DNA/RNA)
non necessarily involving living matter

Molecular Programming: The Hardware Aspect

Smaller and smaller things can be built

Smaller and Smaller

Very few Moore's cycles left!

First working transistor

John Bardeen and Walter Brattain, Dec. 23, 1947

First integrated circuit

Jack Kilby, Sep. 1958.

50+ years later

Jan 2010 25nm NAND flash

Intel&Micron. ~50atoms

Jun 2018 7nm (54nm pitch)

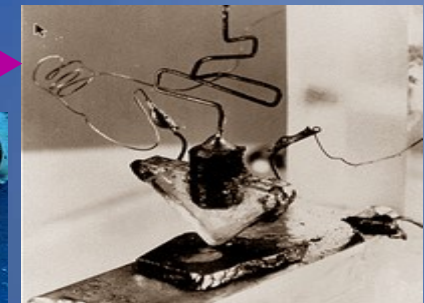
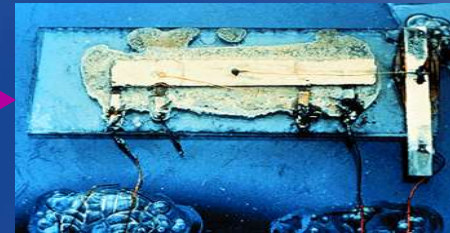
TSMC, Intel, Samsung, GlobalFoundries - mass production

Single molecule transistor

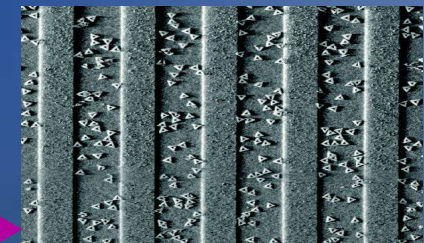
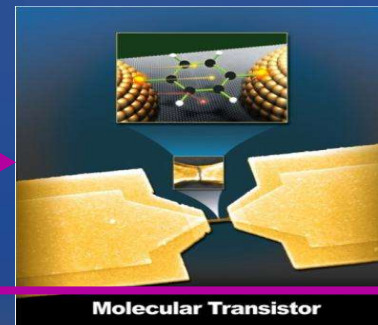
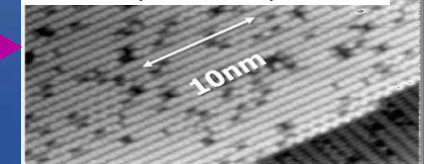
Observation of molecular orbital gating

Nature, 2009; 462 (7276): 1039

Molecules on a chip



Scanning tunneling microscope image of a silicon surface: 10nm is ~20 atoms (in cubic lattice)



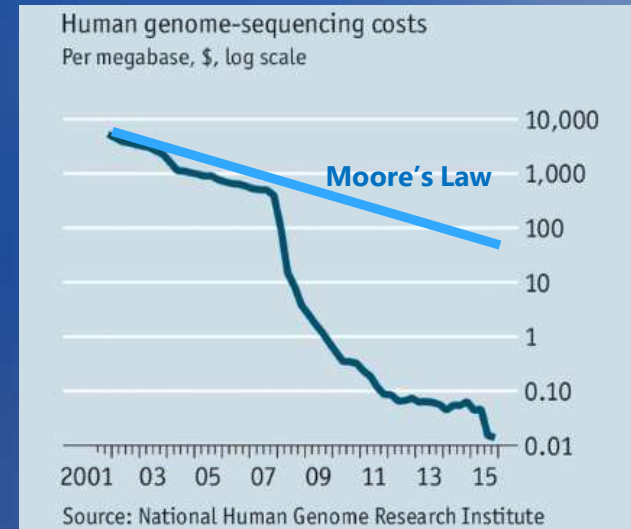
Placement and orientation of individual DNA shapes on lithographically patterned surfaces. *Nature Nanotechnology* 4, 557 - 561 (2009).

Race to the Bottom

Moore's Law is approaching the single-molecule limit

Carlson's Curve is the new exponential growth curve in technology

In both cases, we are now down to *molecules*



The Pace and Proliferation of Biological Technologies

March 4, 2004 by Rob Carlson

Waiter! There is fly DNA in my soup!

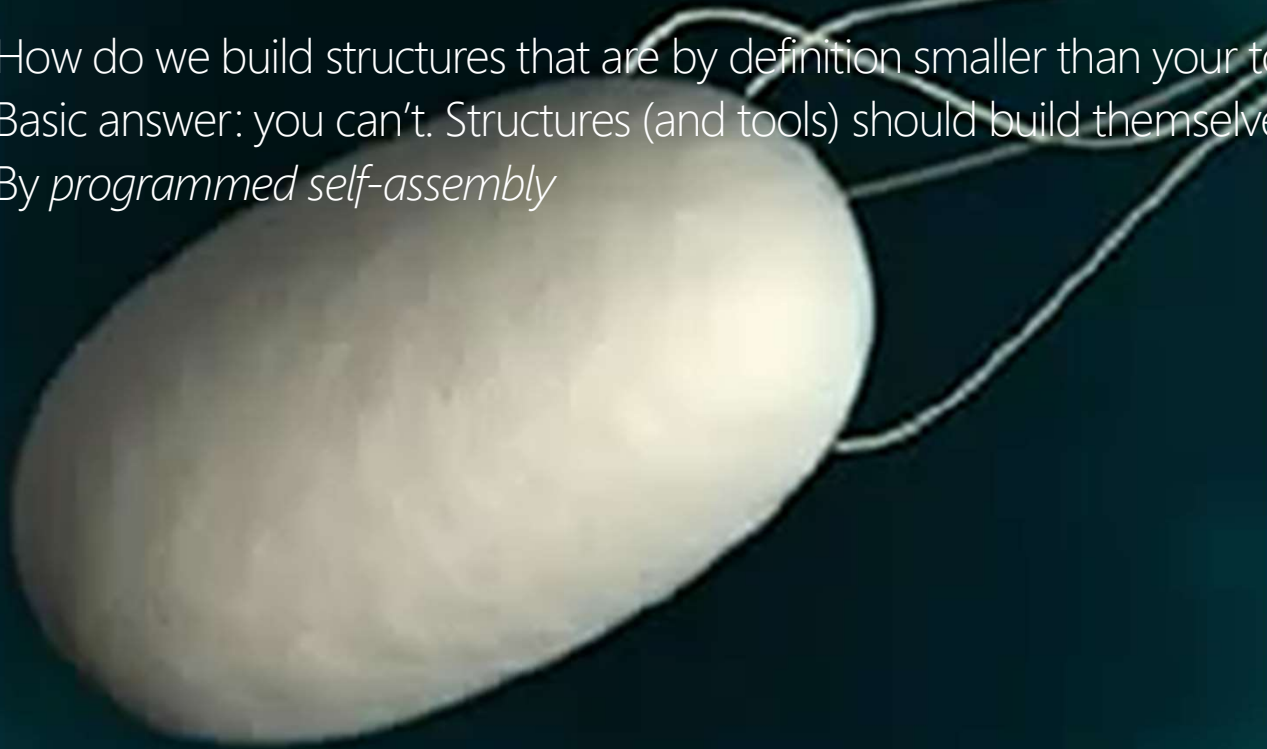
The SmidgION: A portable DNA sequencer that runs on an iPhone

Oxford Nanopore



Building the *Smallest Things*

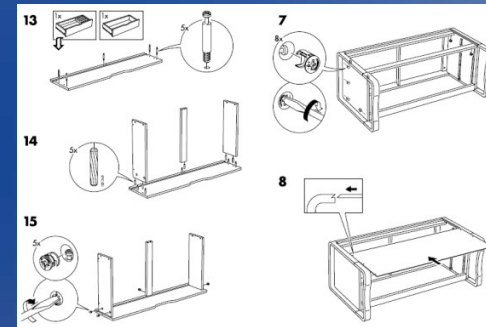
- How do we build structures that are by definition smaller than your tools?
- Basic answer: you can't. Structures (and tools) should build themselves!
- By *programmed self-assembly*



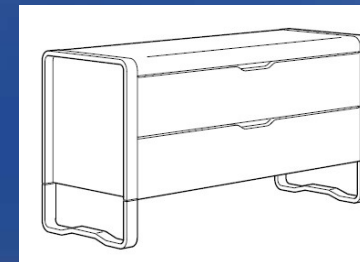
www.youtube.com/watch?v=Ey7Emddf7Y

Molecular IKEA

- Nature can self-assemble.
Can we?
- "Dear IKEA, please send me a chest of drawers that assembles itself."
- We need a magical material where the pieces are pre-programmed to fit into to each other.
- At the molecular scale many such materials exist...



↓ Add water



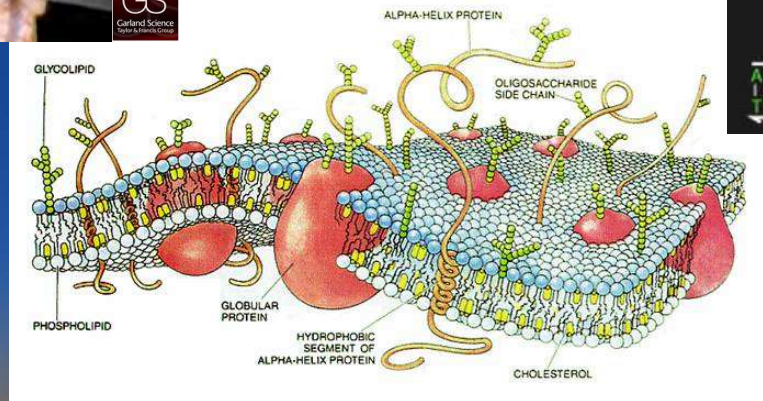
http://www.ikea.com/ms/en_US/customer_service/assembly_instructions.html

Programmed Self-Assembly

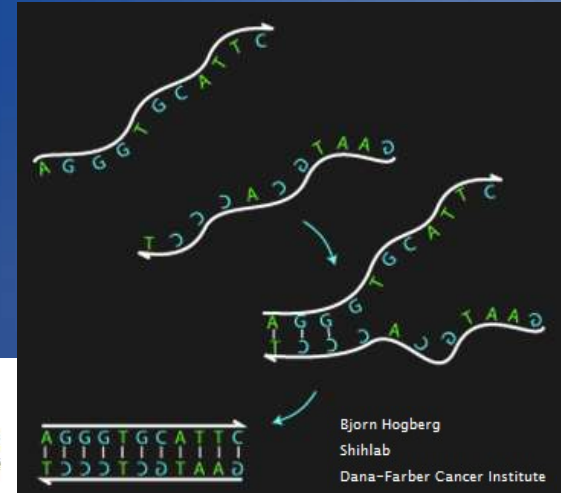
Proteins



Membranes



DNA/RNA



Molecular Programming: The Software Aspect

Smaller and smaller things can be programmed

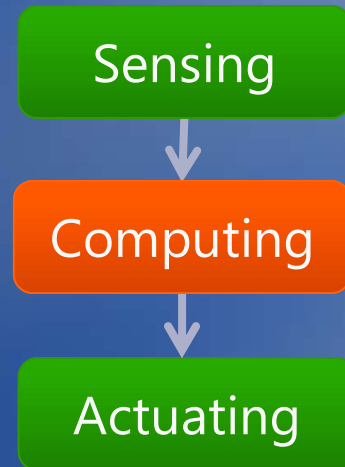
We can program...

- Information
 - Completely!



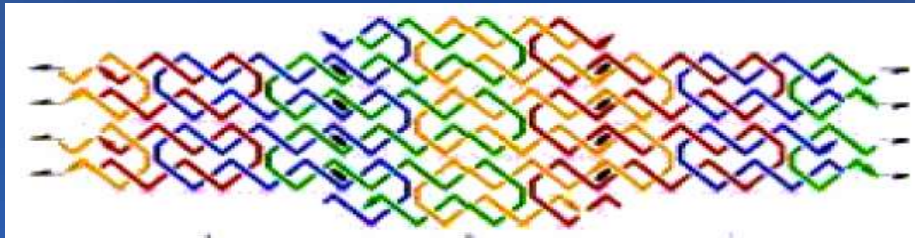
We can program...

- Forces
 - Completely!
(Modulo sensors/actuators)

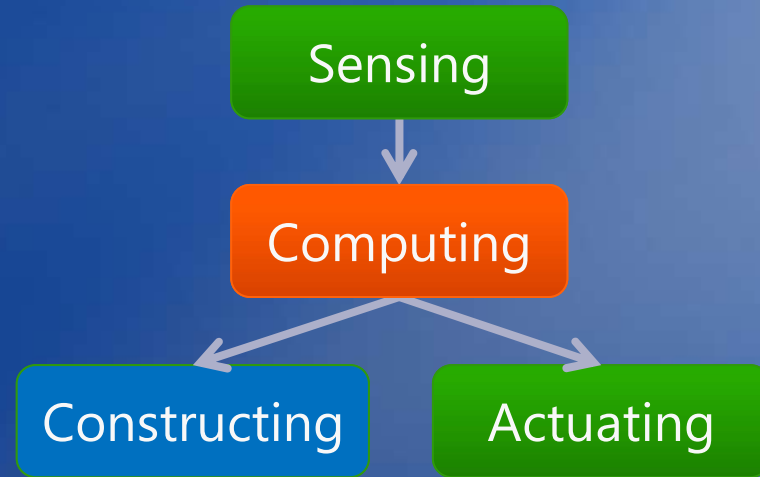


We can program...

- Matter
 - Completely and directly! By self-assembly.
 - Currently: only DNA/RNA.

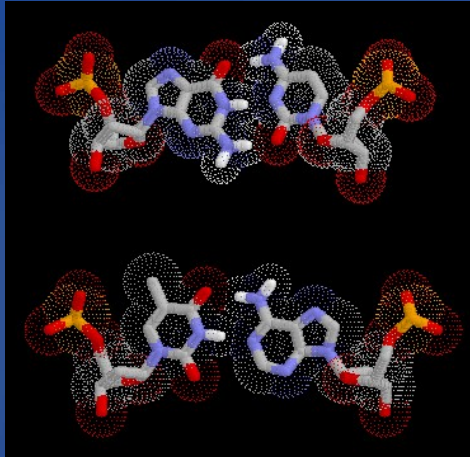


- But DNA is an amazing *material*



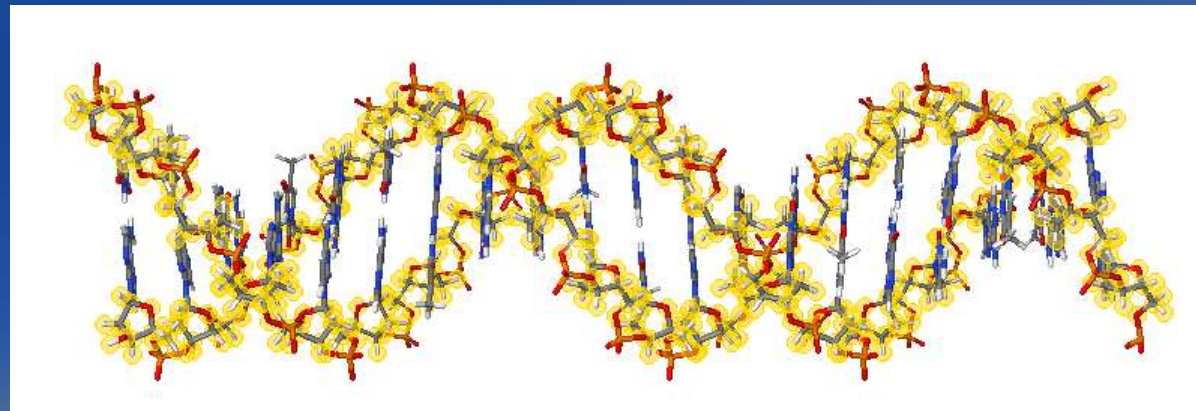
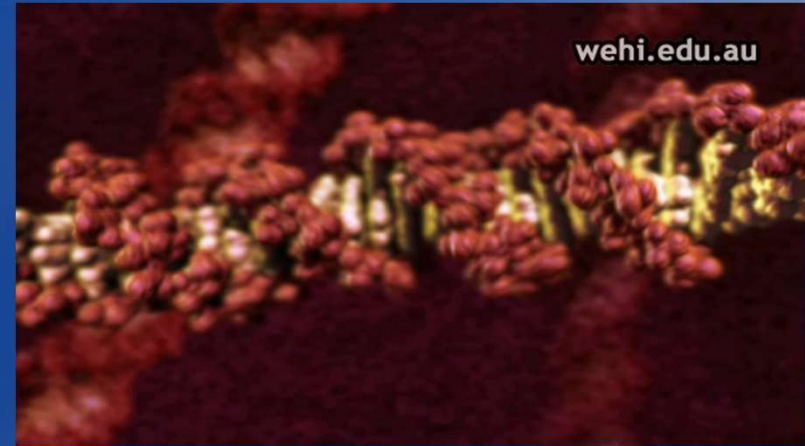
It's like a 3D printer without the printer!
[Andrew Hellington]

DNA



G-C Base Pair
Guanine-Cytosine

T-A Base Pair
Thymine-Adenine



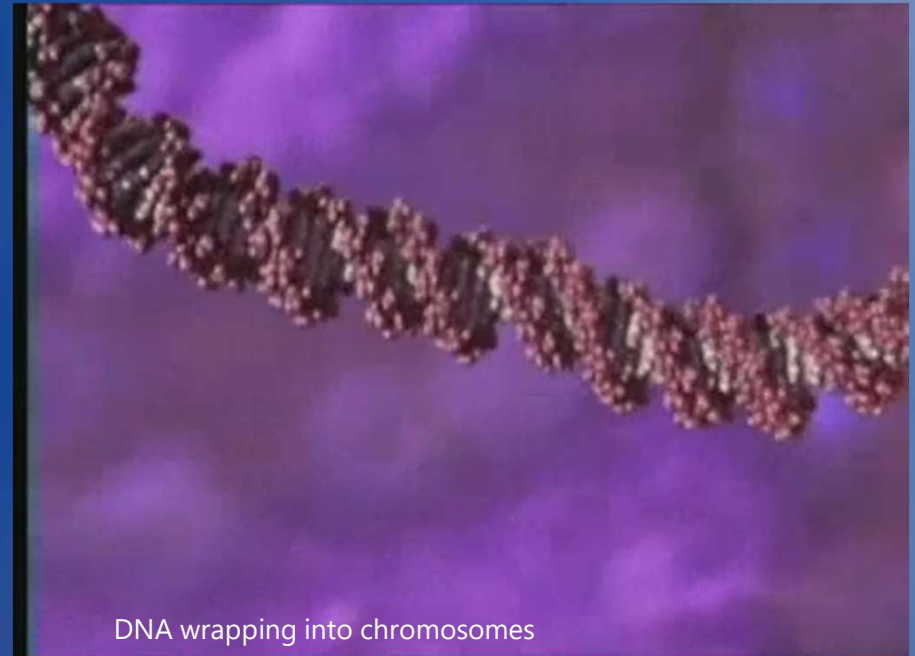
Sequence of Base Pairs (GACT alphabet)

[Interactive DNA Tutorial](http://www.biosciences.bham.ac.uk/labs/minchin/tutorials/dna.html)

(<http://www.biosciences.bham.ac.uk/labs/minchin/tutorials/dna.html>)

DNA Specs

- DNA in each human cell
 - 3 billion base pairs
 - 2nm thick = 4 silicon atoms (in silicon lattice)!
 - 0.34nm per basepair = 2 bits in 2/3 silicon atom!
 - 2 meters long
 - copied in parallel at each cell division!
 - 750 megabytes
 - 80% functional, but only 1.5% protein coding
 - folded into a 6 μ m spherical nucleus
 - = 140 exabytes (million terabytes)/mm³
 - => all the data on the internet fits in a shoebox!
- DNA in each human body
 - 10 trillion cells
 - 133 Astronomical Units long
 - 7.5 octabytes (replicated)
- DNA in human population
 - 20 million light years long

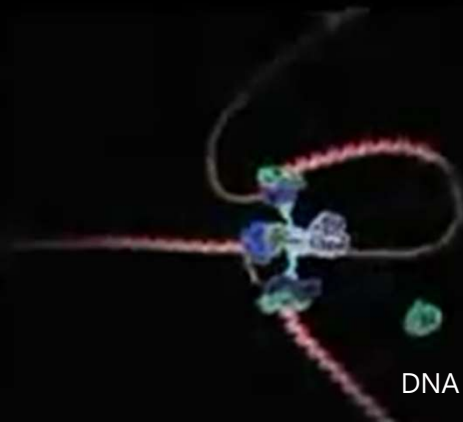


DNA wrapping into chromosomes



Andromeda Galaxy
2.5 million light years away

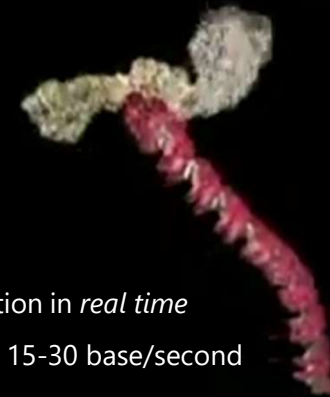
DNA Benchmarks



DNA replication in *real time*

In Humans: 50 nucleotides/second
Whole genome in a few hours (with parallel processing)

In Bacteria: 1000 nucleotides/second
(higher error rate)



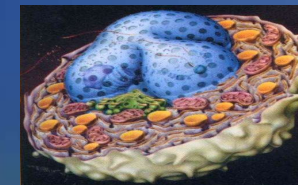
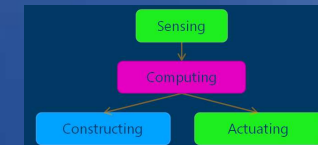
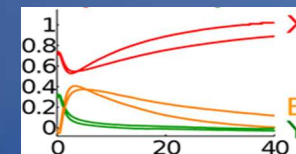
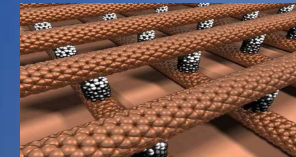
DNA transcription in *real time*

RNA polymerase II: 15-30 base/second

Drew Berry
<http://www.wehi.edu.au/wehi-tv>

One molecule to rule them all

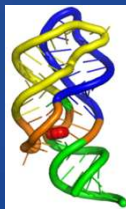
- There are many, many nanofabrication techniques and materials
- But only DNA (and RNA) can:
 - Organize ANY other matter [caveats apply]
 - Execute ANY kinetics [caveats: up to time scaling]
 - Assemble Nano-Control Devices
 - Interface to Biology



H.Lodish & al. Molecular Cell Biology, 4th ed.

Building Nano-Control Devices

All the components of nanocontrollers can already be built entirely and solely with DNA, and interfaced to the environment



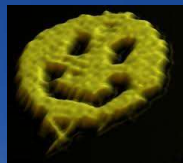
DNA Aptamers

Sensing

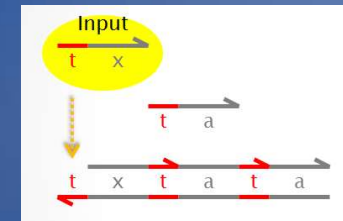
Computing

Constructing

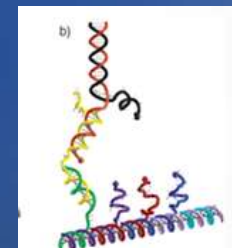
Actuating



Self-assembling DNA Tiles

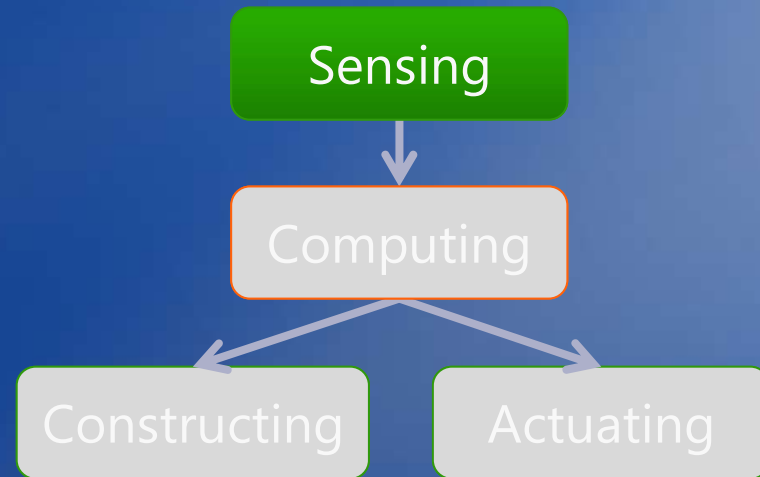


DNA Logical Gates



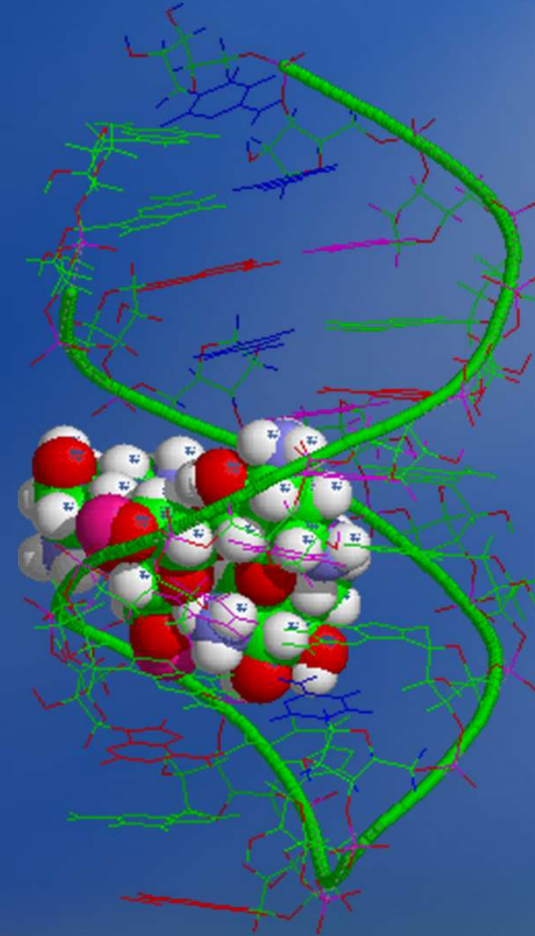
DNA Walkers & Cages

Sensing



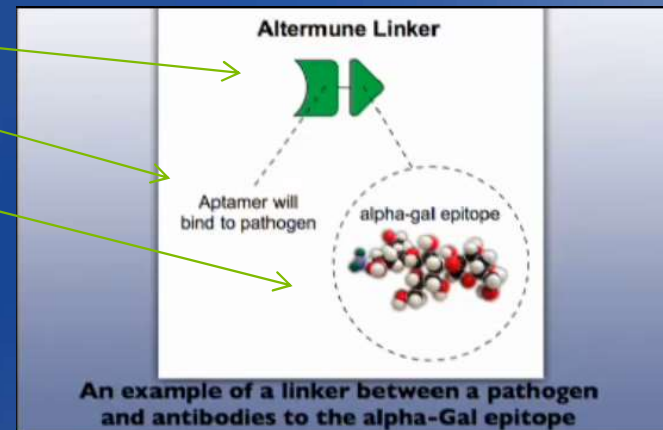
Aptamers

Artificially evolved DNA molecules that stick to (almost) anything you like highly selectively

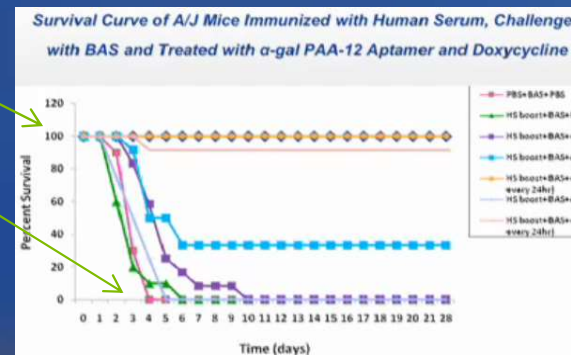


Pathogen Spotlights

- DNA aptamer binds to:
 - A) a pathogen
 - B) a molecule our immune system (when allergic) hates and immediately removes (eats) along with anything attached to it!

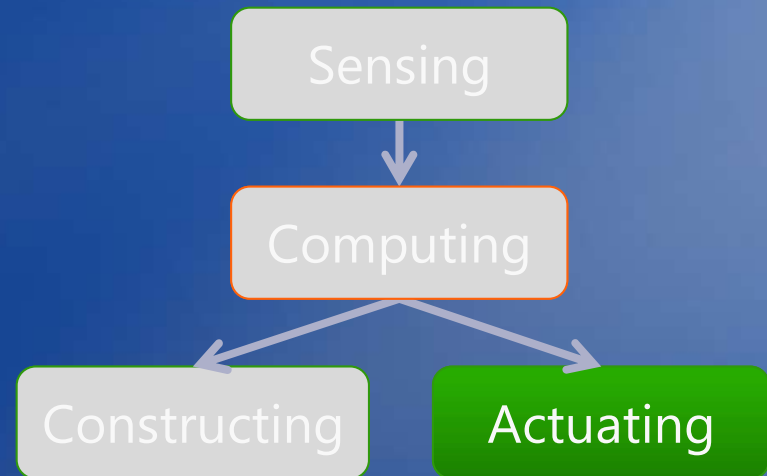


- Result: instant immunity
 - Mice poisoned with Anthrax plus aptamer (100% survival)
 - Mice poisoned with Anthrax (not so good)

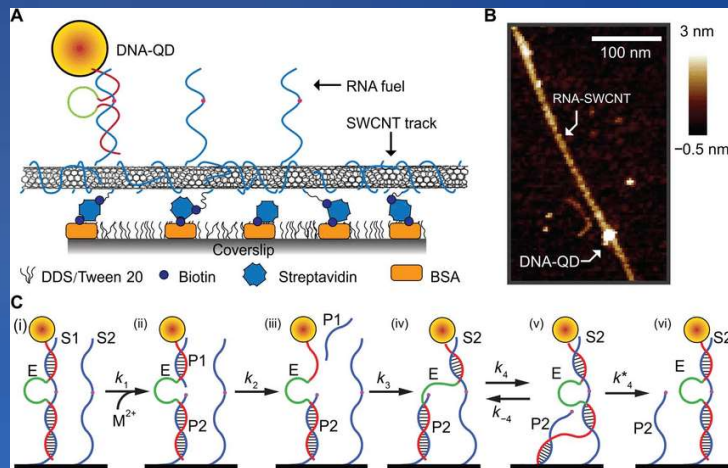
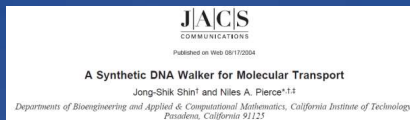


Kary Mullis (incidentally, also Nobel prize for inventing the Polymerase Chain Reaction)

Actuating



DNA Walkers



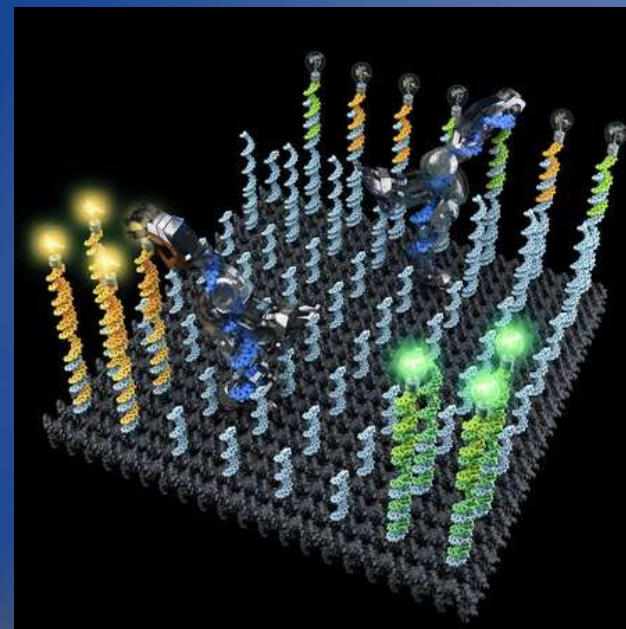
Visible/near-infrared subdiffraction imaging reveals the stochastic nature of DNA walkers

January 2017 · Science Advances 3(1):e1601600
DOI: 10.1126/sciadv.1601600
License: CC BY-NC 4.0

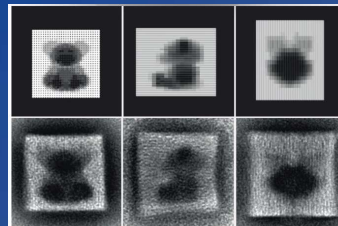
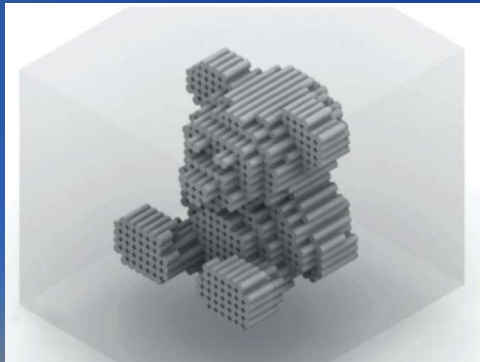
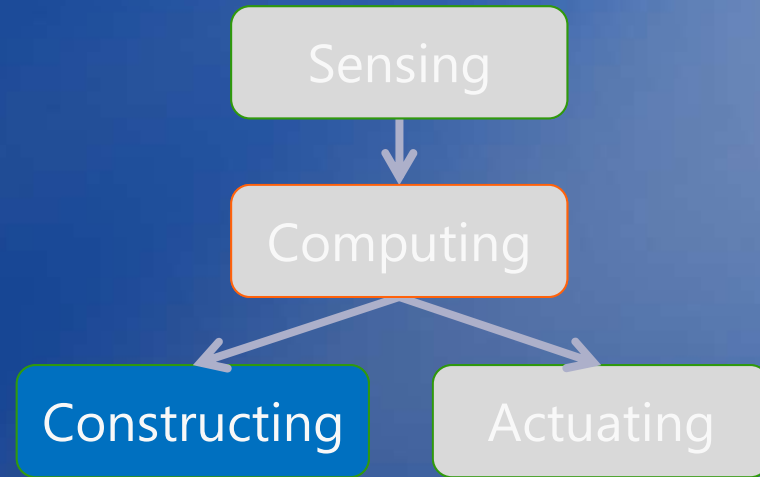
Jing Pan · Tae-Gon Cha · Feiran Li · Show all 6 authors · Jong Hyun Choi

DNA Robotics

A cargo-sorting DNA robot
Thubagere, Anupama J. and Li, Wei and Johnson, Robert F. and Chen, Zibo and Doroudi, Shayan and Lee, Yae Lim and Izatt, Gregory and Wittman, Sarah and Srinivas, Niranjan and Woods, Damien and Winfree, Erik and Qian, Lulu (2017) *A cargo-sorting DNA robot*. Science, 357 (6356). Art. No. eaan6558. ISSN 0036-8075.

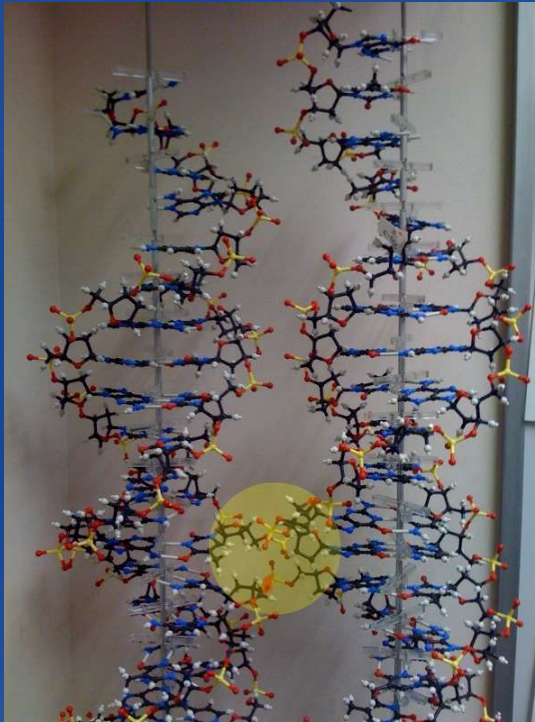
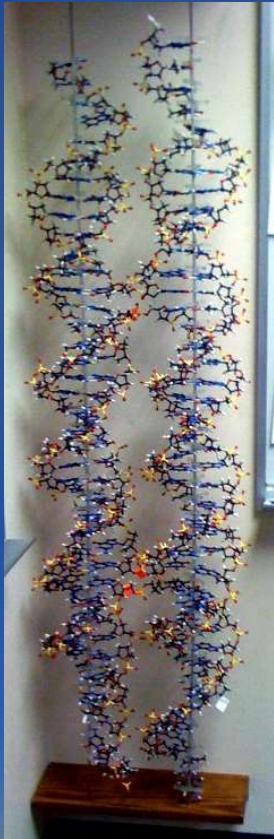


Constructing



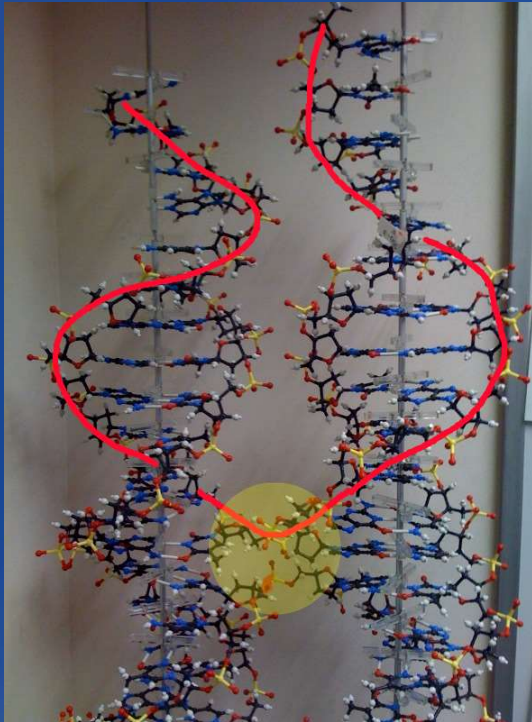
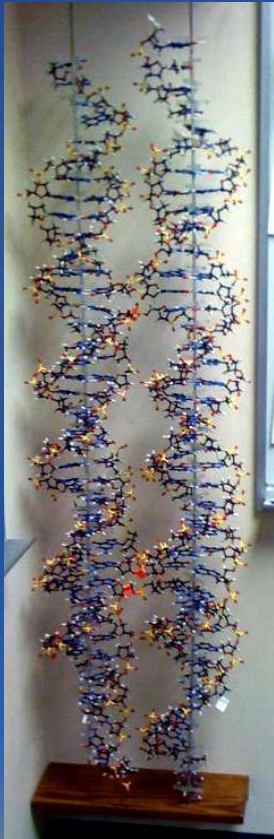
The 3D model of the computer-designed bear shape shown on top was fabricated into the nanostructures visualized with transmission electron microscopy (below). Credit: Wyss Institute at Harvard University

Crosslinking



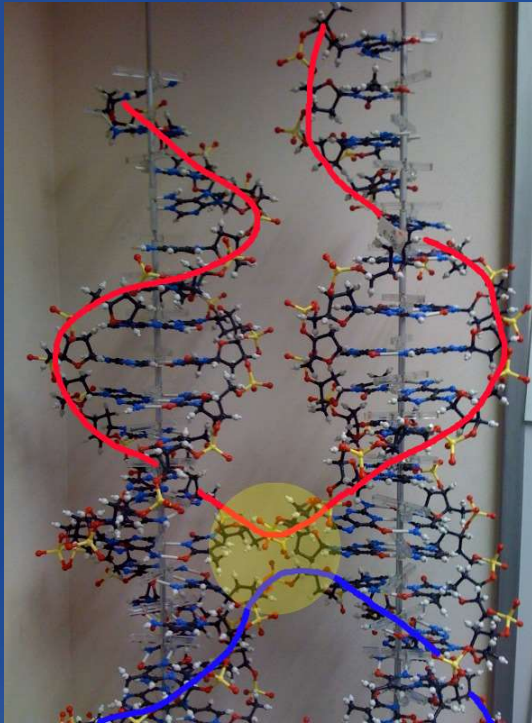
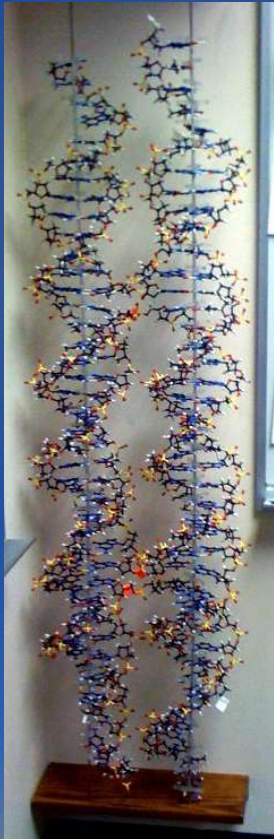
the dawn of
structural DNA
nanotechnology

Crosslinking



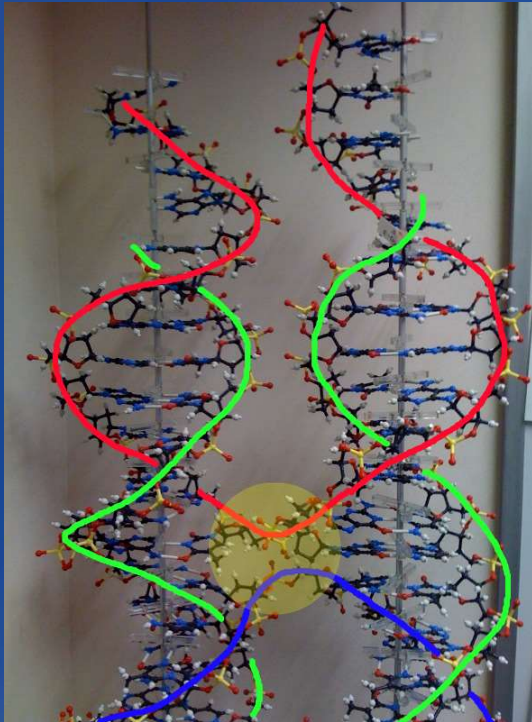
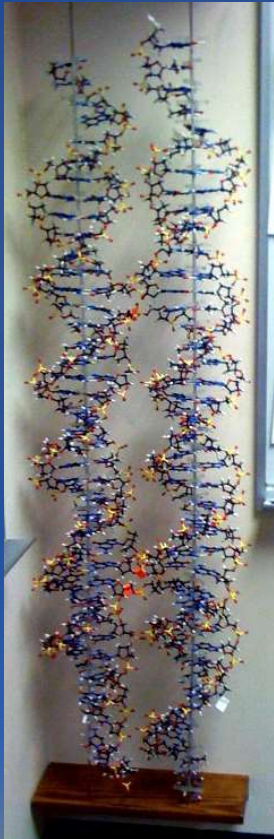
the dawn of
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nanotechnology

Crosslinking



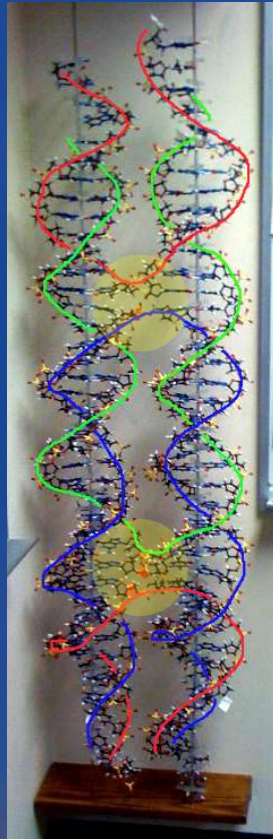
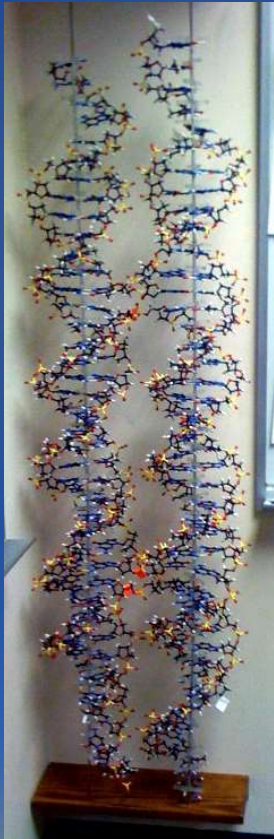
the dawn of
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nanotechnology

Crosslinking

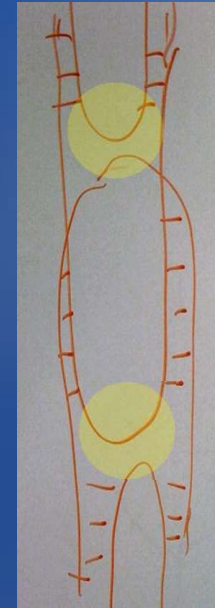


the dawn of
structural DNA
nanotechnology

Crosslinking

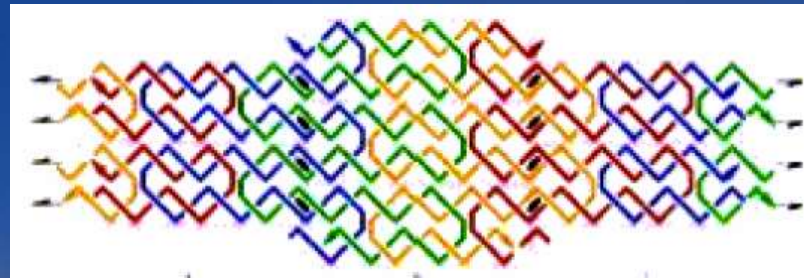
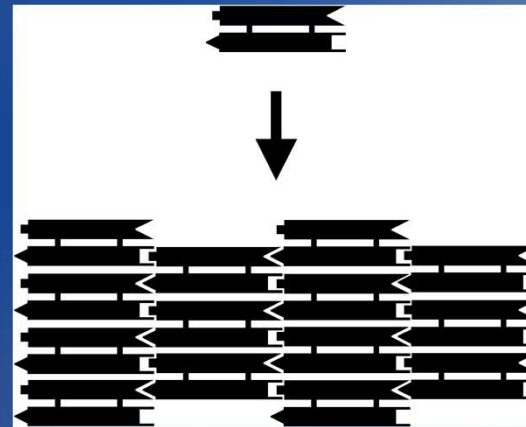
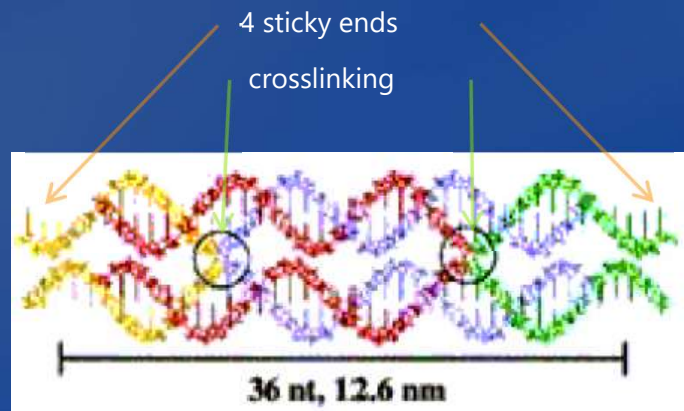


In nature, crosslinking is deadly (blocks DNA replication).



In engineering, crosslinking is the key to using DNA as a construction material.

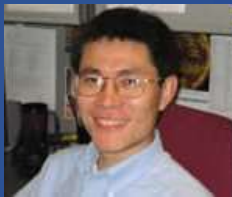
DNA Tiling



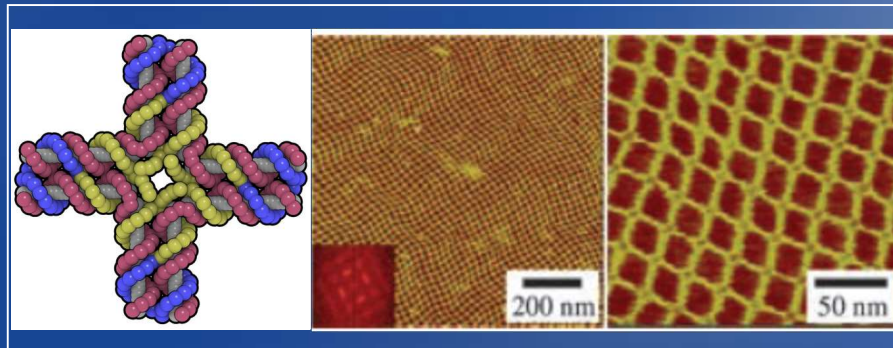
Construction and manipulation of DNA tiles in free space

Pankhudi

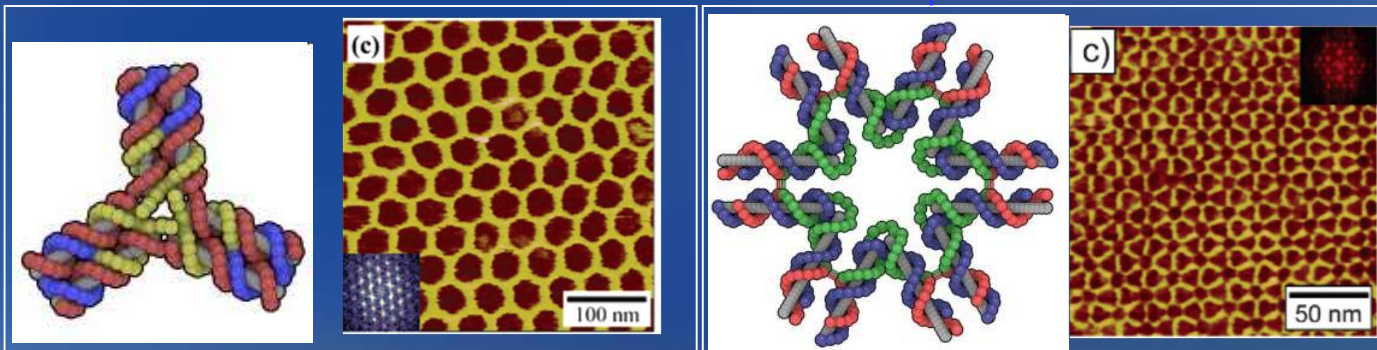
2D DNA Lattices



Chengde Mao
Purdue University, USA



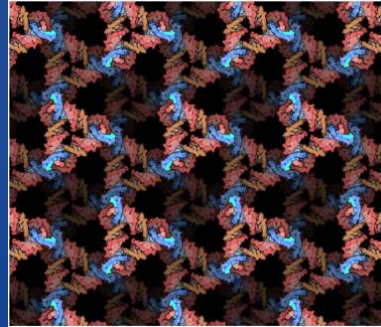
N-point Stars



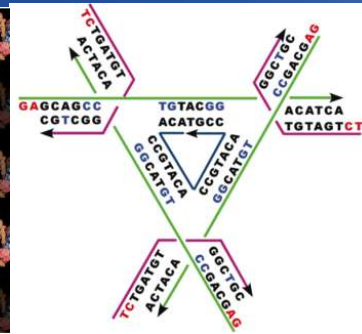
3D DNA Structures



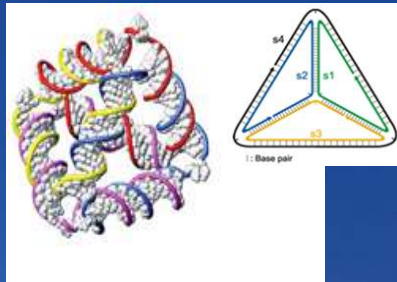
Ned Seeman
NYU



3D Crystal



Andrew Tuberfield
Oxford



Tetrahedron

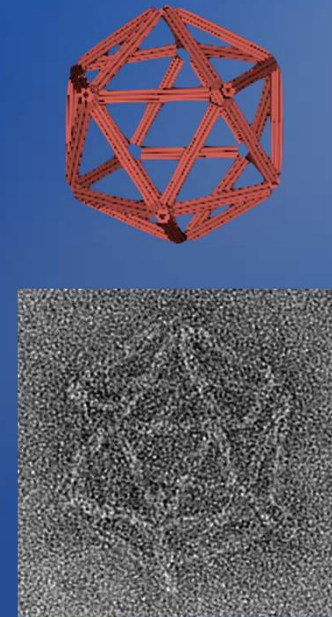
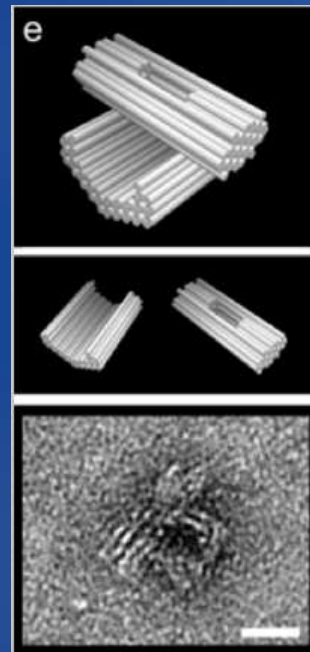
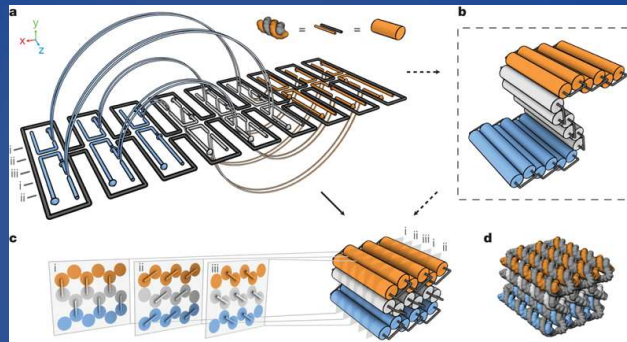


Friedrich Simmel
Munich

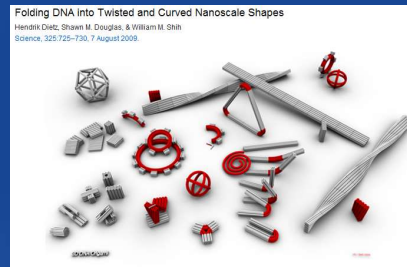


Robotic Arm

CADnano



William Shih
Harvard

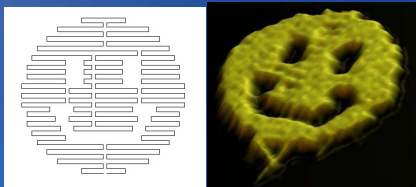


<https://www.youtube.com/watch?v=Ek-FDPymygg>

S.M. Douglas, H. Dietz, T. Liedl, B. Högberg, F. Graf and W. M. Shih
Self-assembly of DNA into nanoscale three-dimensional shapes, Nature (2009)

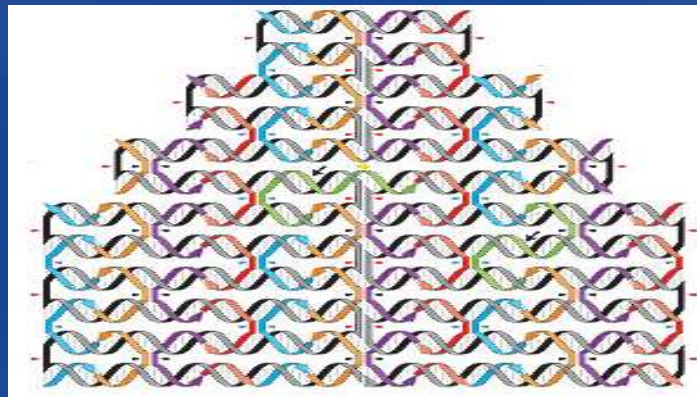
DNA Origami

Folding a long (6407bp) naturally occurring circular ssDNA (from bacteriophage M13) via lots of short 'staple' strands that constrain its shape

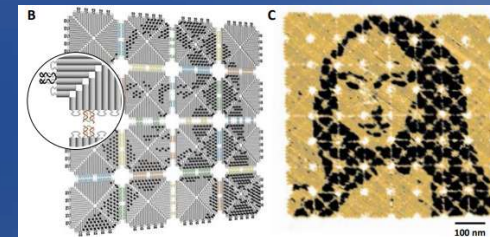


AFM image

Paul Rothemund's
"Disc with three holes" (2006)
Nature 440, 297, 2006



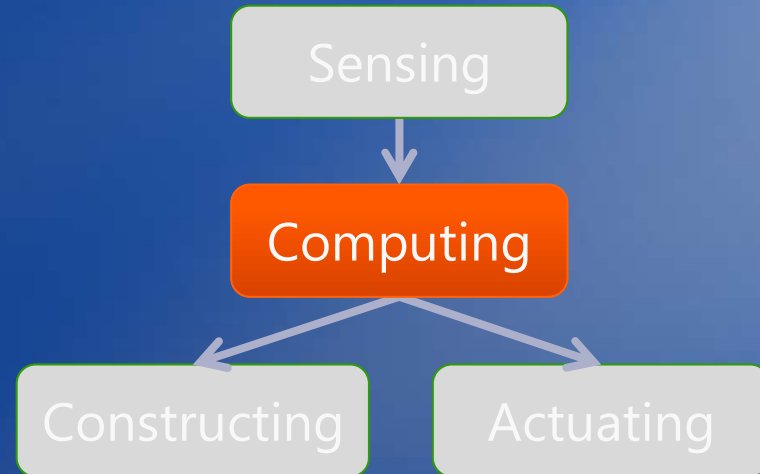
Black/gray: 1 long viral strand (natural DNA)
Color: many short staple strands (synthetic DNA)



AFM image

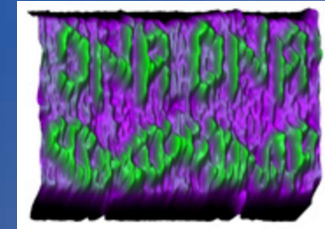
Lulu Qian's
Hierarchical assembly (2017)
Nature, 552(7683):67–71, 2017

Computing



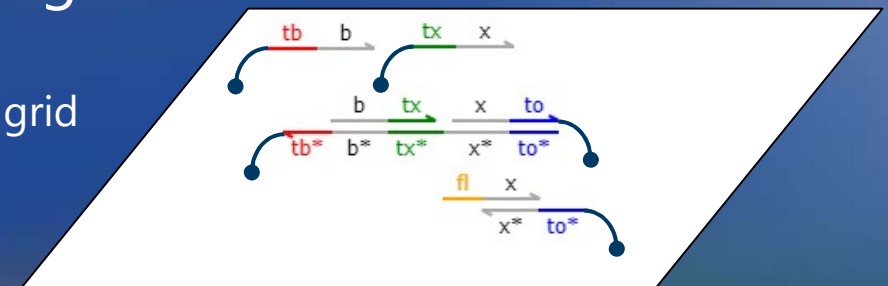
DNA Circuit Boards

- DNA origami are arrays of uniquely-addressable locations
 - Each staple is different and binds to a unique location on the origami
 - It can be extended with a unique sequence so that something else will attach uniquely to it.



Some staples are attached to "green blobs" (as part of their synthesis) Other staples aren't

- More generally, we can bind "DNA gates" to specific locations
 - And so connect them into "DNA circuits" on a grid
 - Only neighboring gates will interact

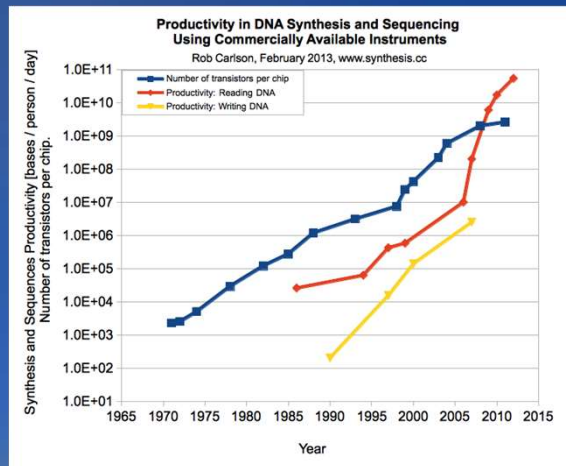


DNA Storage (Read/Write)

Information-rich physical structures can be used for storage.

DNA has a data density of **140 exabytes** (1.4×10^{20} bytes) per mm^3 compared to state-of-the-art storage media that reaches ~ 500 megabytes (5×10^8 bytes) per mm^3

DNA has been shown to be stable for millions of years

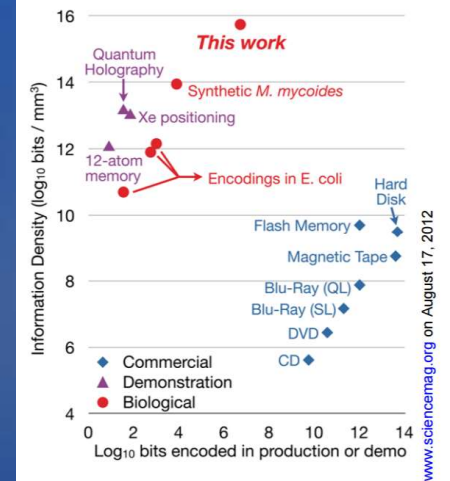


The Pace and Proliferation of Biological Technologies

March 4, 2004 by Rob Carlson

Next-Generation Digital Information Storage in DNA

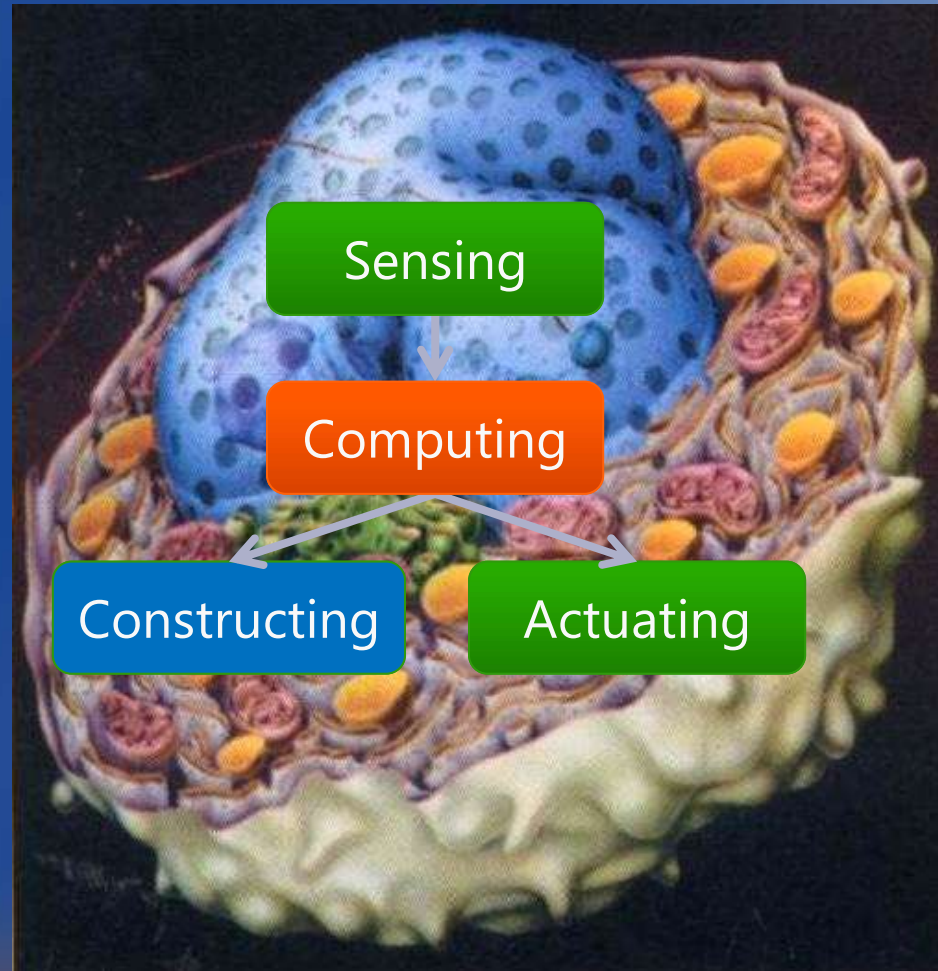
George M. Church,^{1,2} Yuan Gao,³ Sriram Kosuri^{1,2*}



We have machines that can read (sequence) and write (synthesize) DNA. The **Carlson Curve** of "productivity" is growing **much faster than Moore's Law**.

Cost of sequencing is decreasing rapidly (\$1000 whole human genome), while cost of synthesis is decreasing very slowly. [Rob Carlson, www.synthesis.cc]

Curing



Interfacing to Biology

- A doctor in each cell

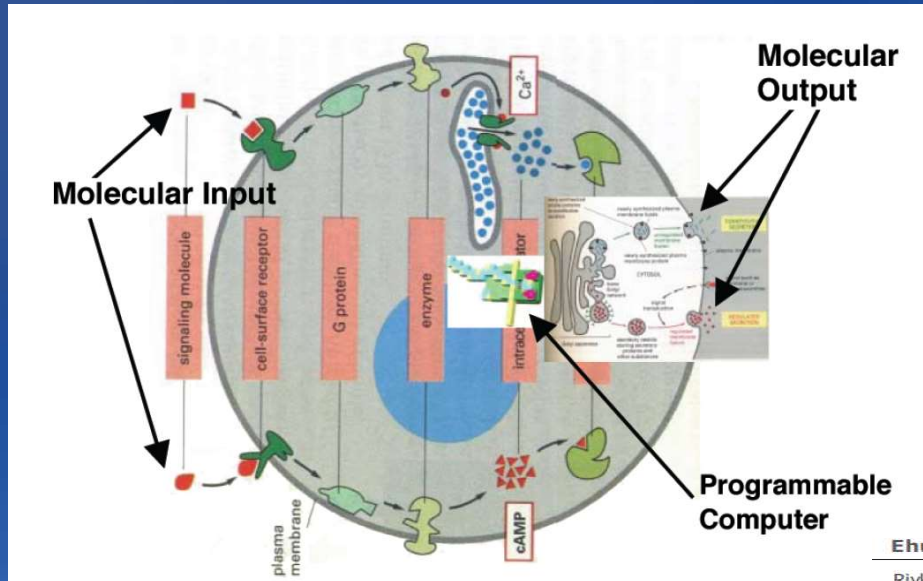


Fig. 1 Medicine in 2050: "Doctor in a Cell"

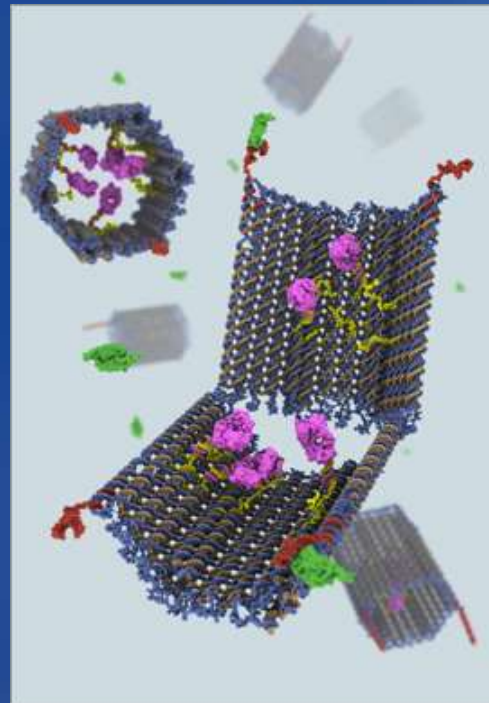
Ehud Shapiro

Rivka Adar
Kobi Benenson
Gregory Linshitz
Aviv Regev
William Silverman

**Molecules and
computation**

~2002

Programmed Drug Delivery



A Logic-Gated Nanorobot for Targeted Transport of Molecular Payloads

Shawn M. Douglas[†], Ido Bachelet[†], George M. Church[†]

[†] See all authors and affiliations

Science 17 Feb 2012:
Vol. 335, Issue 6070, pp. 831-834
DOI: 10.1126/science.1214081

Molecular Programming: The Execution Aspect

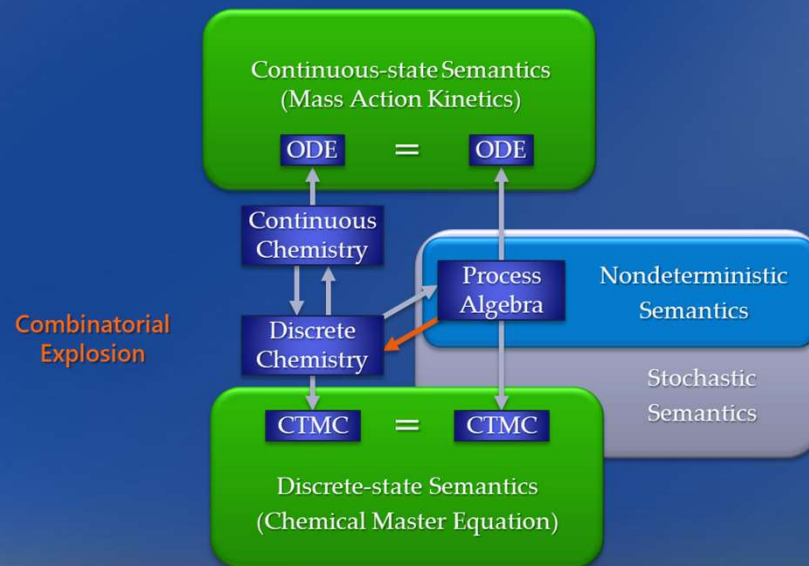
How do we "run" a molecular program?

Programming Language: Chemistry

- A Lingua Franca between Biology, Dynamical Systems, and Concurrent Languages
- Chemical Reaction Networks
 - $A + B \xrightarrow{r} C + D$ (the program)
- Ordinary Differential Equations
 - $d[A]/dt = -r[A][B] \dots$ (the behavior)
- Rich analytical techniques based on Calculus and more recently on stochastic models

Chemistry as a Concurrent Language

- A connection with the theory of concurrency
 - Via Process Algebra and Petri Nets



Chemical Programming Examples

specification

$Y := \min(X1, X2)$

$Y := \max(X1, X2)$

program

$X1 + X2 \rightarrow Y$

$X1 \rightarrow L1 + Y$

$X2 \rightarrow L2 + Y$

$L1 + L2 \rightarrow K$

$Y + K \rightarrow 0$

$\max(X1, X2) =$
 $(X1 + X2) - \min(X1, X2)$

(but is not computed
"sequentially": it is a form
of concurrent computation)

chemical reaction network

Chemical Reaction Networks

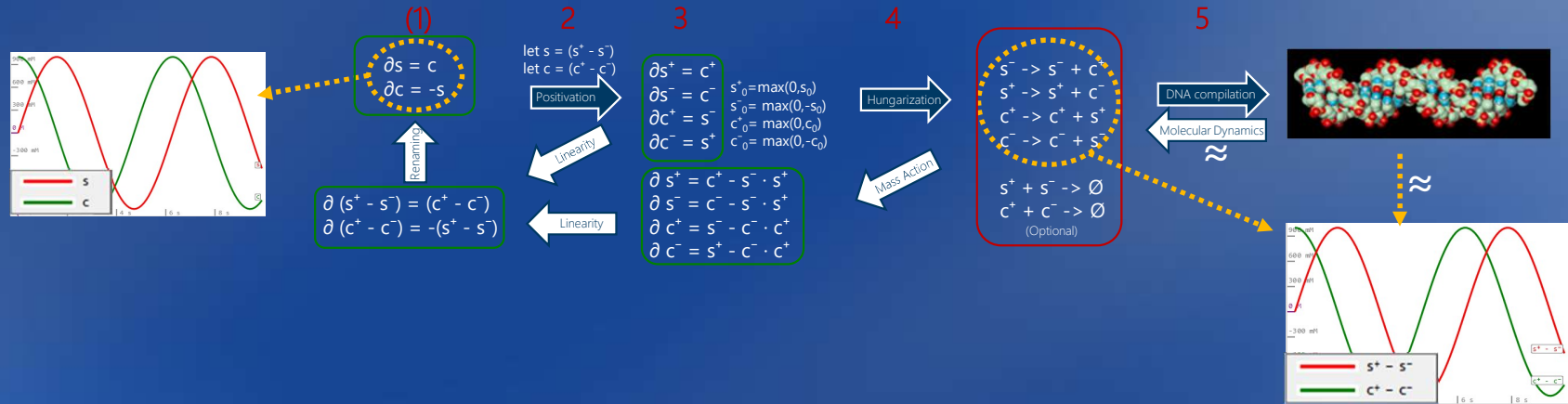
- Finite list of chemical reactions over a finite set of species
 - N.B.: "abstract" species, not specific atoms/molecules that physically exist
- Computationally Powerful
 - Turing-complete up to an arbitrarily small error
- Full Turing Completeness
 - When including complexation (polymerization), which DNA enables (complexation encodes an actual infinity of chemical reactions by finite means)

Programming ^{“elementary”} any dynamical system as a CRN

For example, take *the* canonical oscillator: sine/cosine

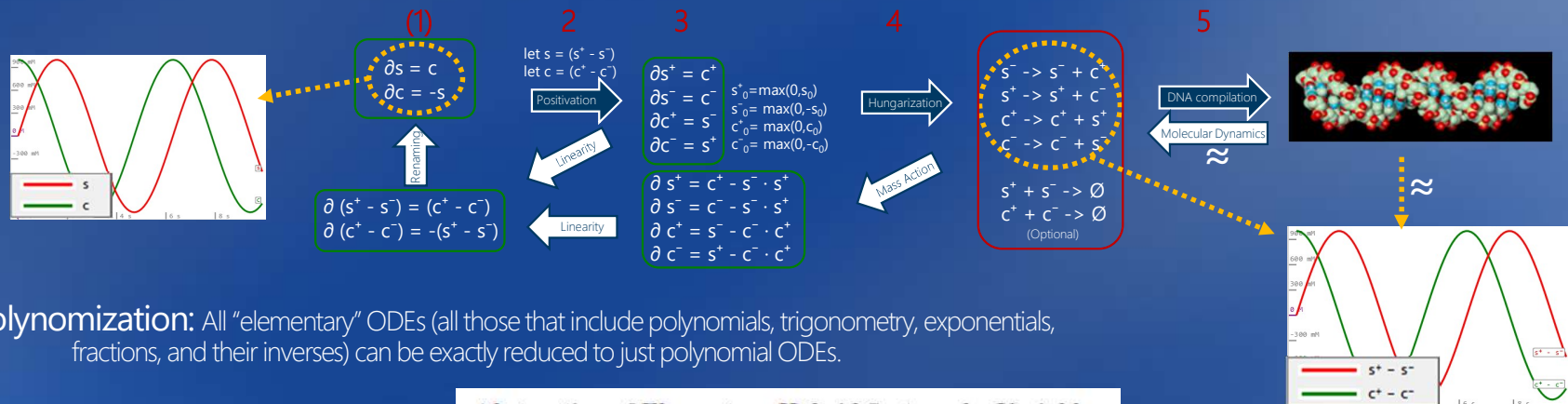
$$\partial^2 \theta = -g/l \sin \theta$$

Equation of motion of a simple pendulum



Programming ^{“elementary”} any dynamical system as a CRN

For example, take *the* canonical oscillator: sine/cosine

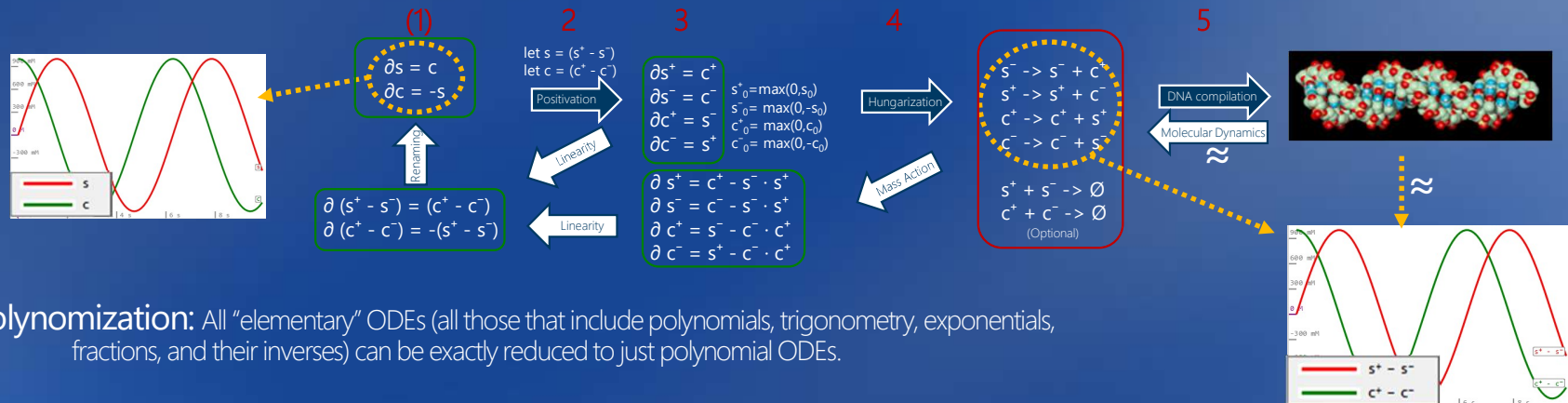


Abstraction of Elementary Hybrid Systems by Variable Transformation

Jiang Liu¹, Naijun Zhan², Hengjun Zhao¹, and Liang Zou²

Programming ^{“elementary”} any dynamical system as a CRN

For example, take *the* canonical oscillator: sine/cosine



1. **Polynomization:** All “elementary” ODEs (all those that include polynomials, trigonometry, exponentials, fractions, and their inverses) can be exactly reduced to just polynomial ODEs.

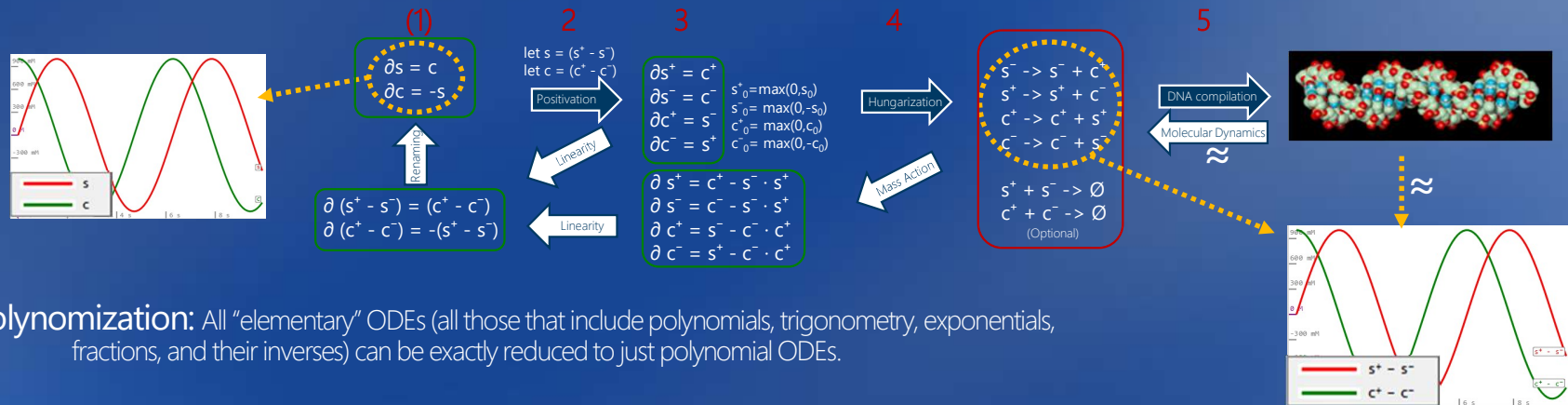
2. **Positivation:** All polynomial ODEs can be exactly reduced to polynomial ODEs in the positive quadrant (as differences).

Biomolecular implementation of linear I/O systems

K. Oishi E. Klavins

Programming ^{“elementary”} *any* dynamical system as a CRN

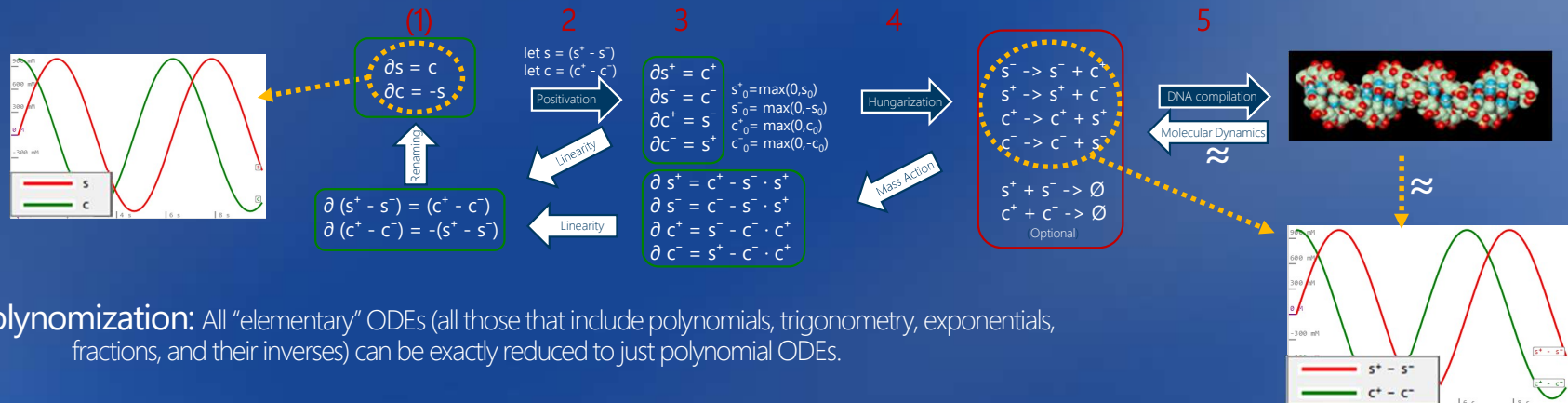
For example, take *the* canonical oscillator: sine/cosine



- 1. Polynomization:** All “elementary” ODEs (all those that include polynomials, trigonometry, exponentials, fractions, and their inverses) can be exactly reduced to just polynomial ODEs.
- 2. Positivation:** All polynomial ODEs can be exactly reduced to polynomial ODEs in the positive quadrant (as differences).
- 3. All positivized ODEs are Hungarian:** I.e., all negative monomials have their l.h.s. differential variable as a factor.

Programming ^{“elementary”} *any* dynamical system as a CRN

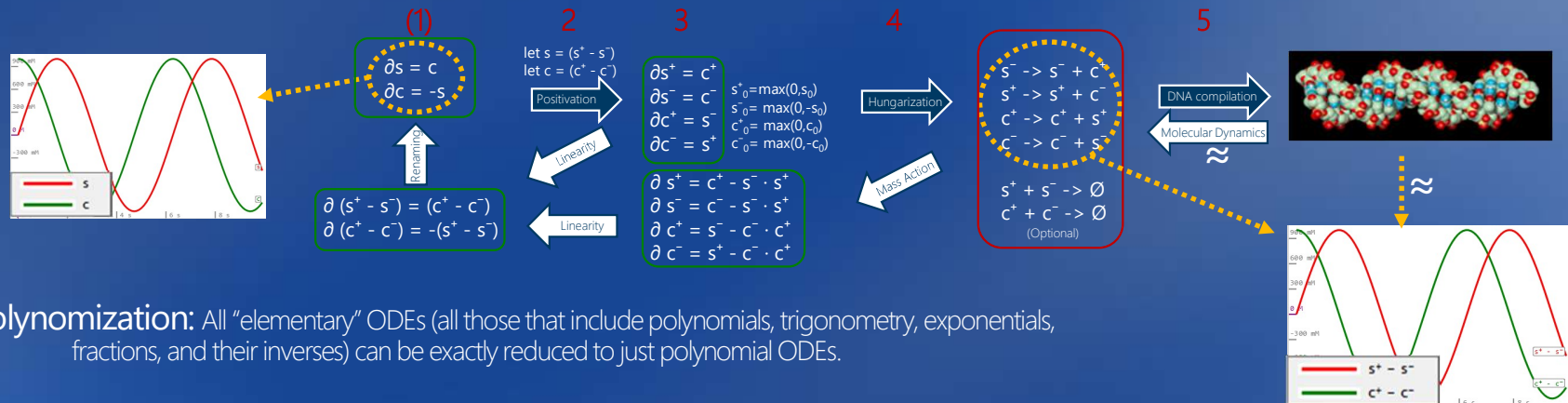
For example, take *the* canonical oscillator: sine/cosine



- 1. Polynomization:** All “elementary” ODEs (all those that include polynomials, trigonometry, exponentials, fractions, and their inverses) can be exactly reduced to just polynomial ODEs.
- 2. Positivation:** All polynomial ODEs can be exactly reduced to polynomial ODEs in the positive quadrant (as differences).
- 3. All positivized ODEs are Hungarian:** I.e., all negative monomials have their l.h.s. differential variable as a factor.
- 4. Hungarization:** All Hungarian ODEs can be exactly reduced to mass action CRNs.

Programming ^{“elementary”} any dynamical system as a CRN

For example, take *the* canonical oscillator: sine/cosine



1. **Polynomization:** All “elementary” ODEs (all those that include polynomials, trigonometry, exponentials, fractions, and their inverses) can be exactly reduced to just polynomial ODEs.

2. **Positivation:** All polynomial ODEs can be exactly reduced to polynomial ODEs in the positive quadrant (as differences).

3. All positivized ODEs are **Hungarian**: I.e., all negative monomials have their l.h.s. differential variable as a factor.

4. **Hungarization:** All Hungarian ODEs can be exactly reduced to mass action CRNs.

5. **Molecular Programming:** All mass action CRNs, up to time rescaling, can be arbitrarily approximated by engineered DNA molecules.

DNA as a universal substrate for chemical kinetics

David Soloveichik, Georg Seelig, and Erik Winfree
 PNAS March 23, 2010 107 (12) 5393-5398; <https://doi.org/10.1073/pnas.0909380107>

How do we “run” Chemistry?

- Chemistry is not easily executable
 - “Please Mr Chemist, execute me this bunch of reactions that I just made up”
- Most molecular languages are not executable
 - They are **descriptive** (modeling) languages
- How can we **execute** molecular languages?
 - With real molecules?
 - That we can design ourselves?
 - And that we can buy on the web?

BREAK



DNA Strand Displacement

An "unnatural" use of DNA for emulating
any system of chemical reactions
with real molecules

Domains

- Subsequences on a DNA strand are called **domains**
 - *provided* they are "independent" of each other
- Differently named domains must not **hybridize**
 - With each other, with each other's complement, with subsequences of each other, with concatenations of other domains (or their complements), etc.

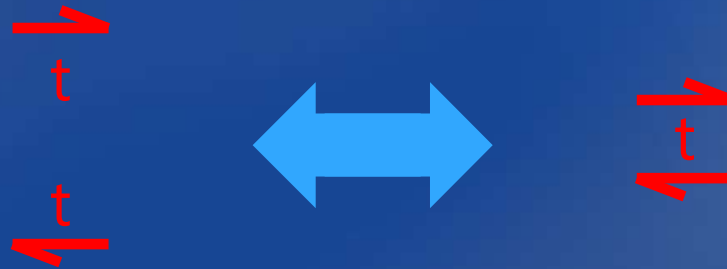
CTTGAGAATCGGATATTCGGATCGCGATTAATCAAATG



x y z

oriented DNA
single strand

Short Domains



DNA double
strand

Reversible Hybridization

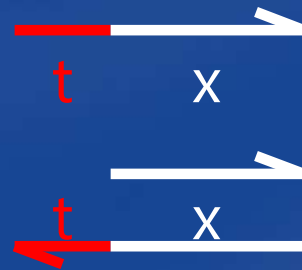
Long Domains



Irreversible Hybridization

Strand Displacement

Strand Displacement



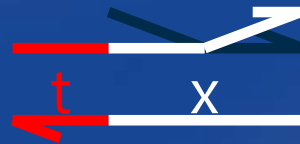
“Toehold Mediated”

Strand Displacement



Toehold Binding

Strand Displacement



Branch Migration

Strand Displacement



Displacement

Strand Displacement

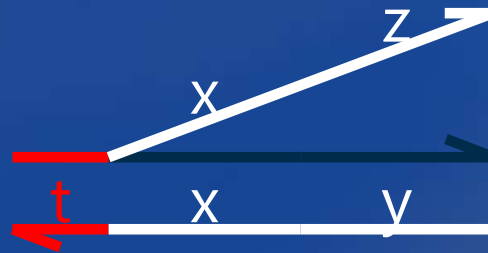


Irreversible release

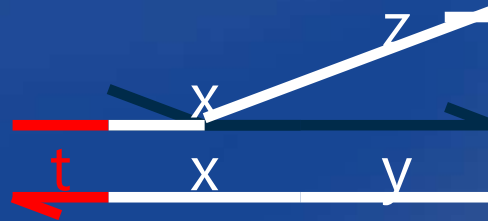
Bad Match



Bad Match



Bad Match



Bad Match



Cannot proceed
Hence will undo

Two-Domain Architecture

- Signals: 1 toehold + 1 recognition region



- Gates: "top-nicked double strands" with open toeholds



Garbage collection
"built into" the gate
operation

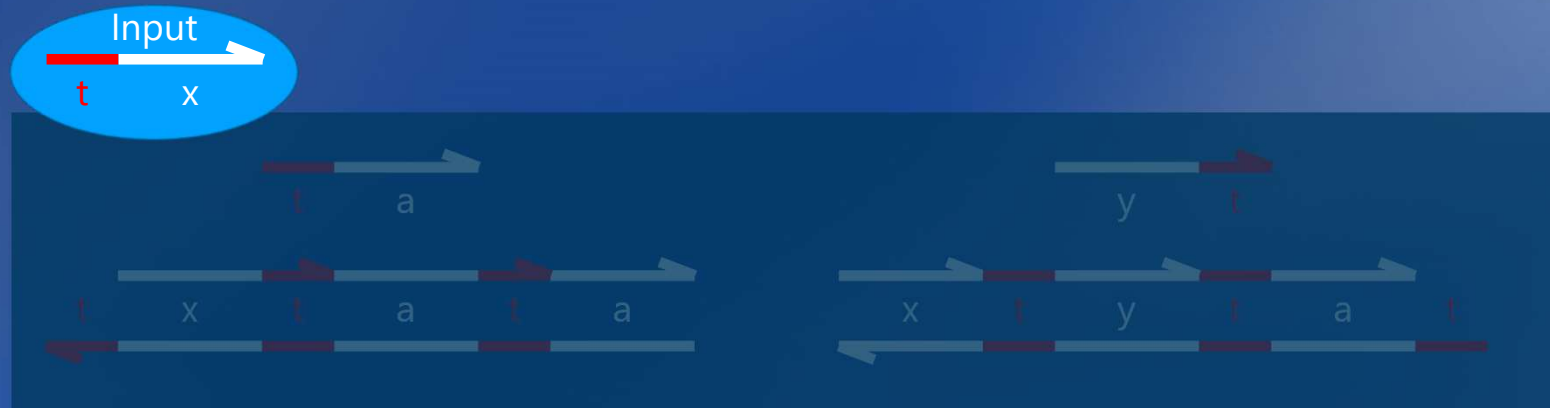
Two-Domain DNA Strand Displacement

Luca Cardelli

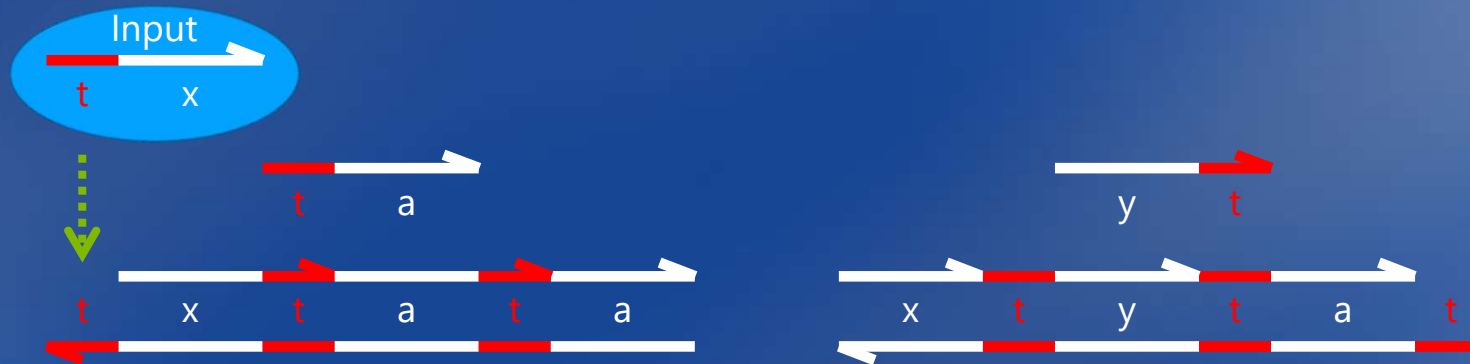
In S. B. Cooper, E. Kashefi, P. Panangaden (Eds.):
Developments in Computational Models (DCM 2010).
EPTCS 25, 2010, pp. 33-47. May 2010.

Transducer

Transducer $x \rightarrow y$



Transducer $x \rightarrow y$



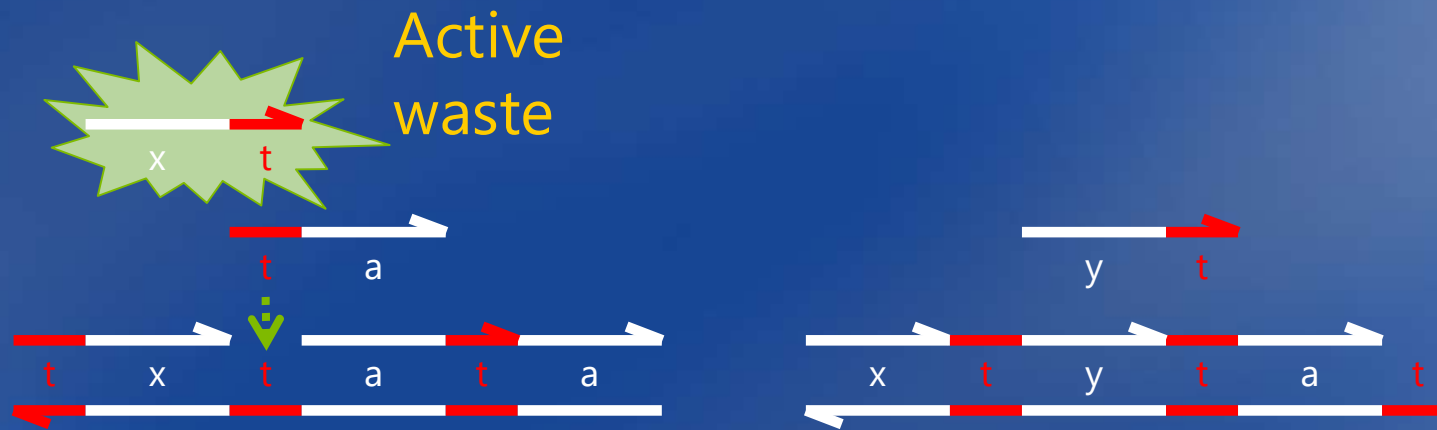
Built by self-assembly!

ta is a *private* signal (a different 'a' for each xy pair)

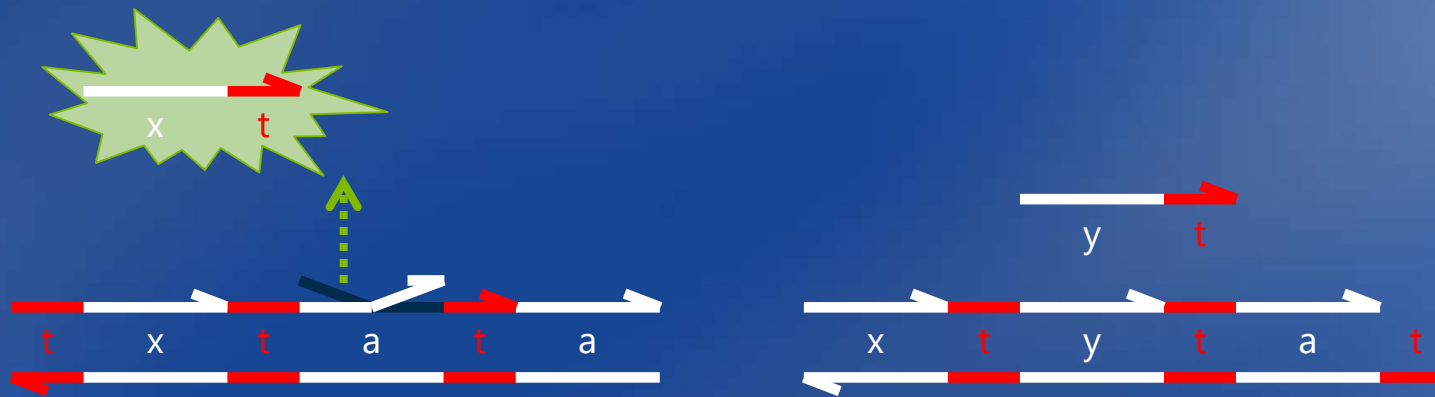
Transducer $x \rightarrow y$



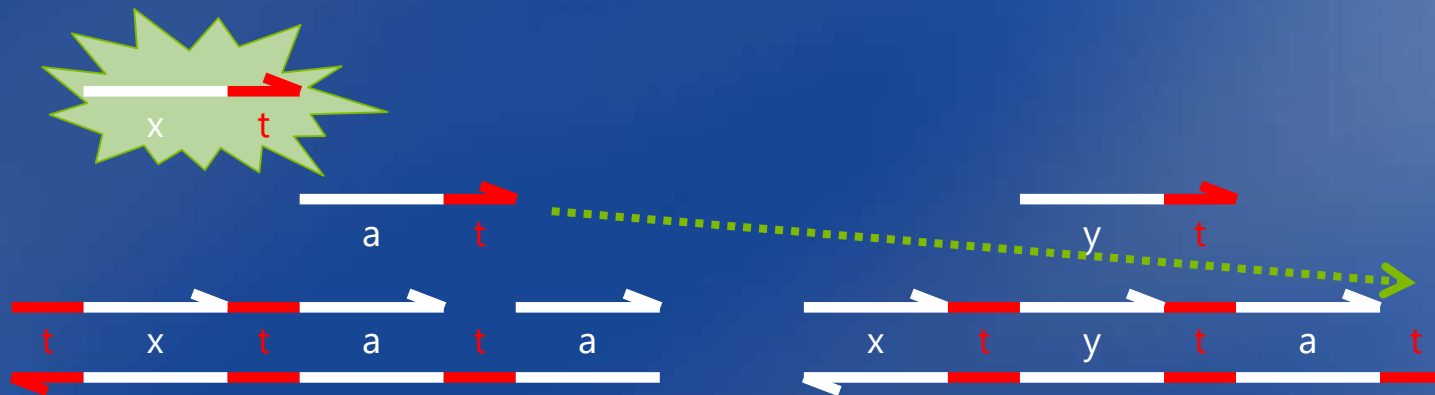
Transducer $x \rightarrow y$



Transducer $x \rightarrow y$

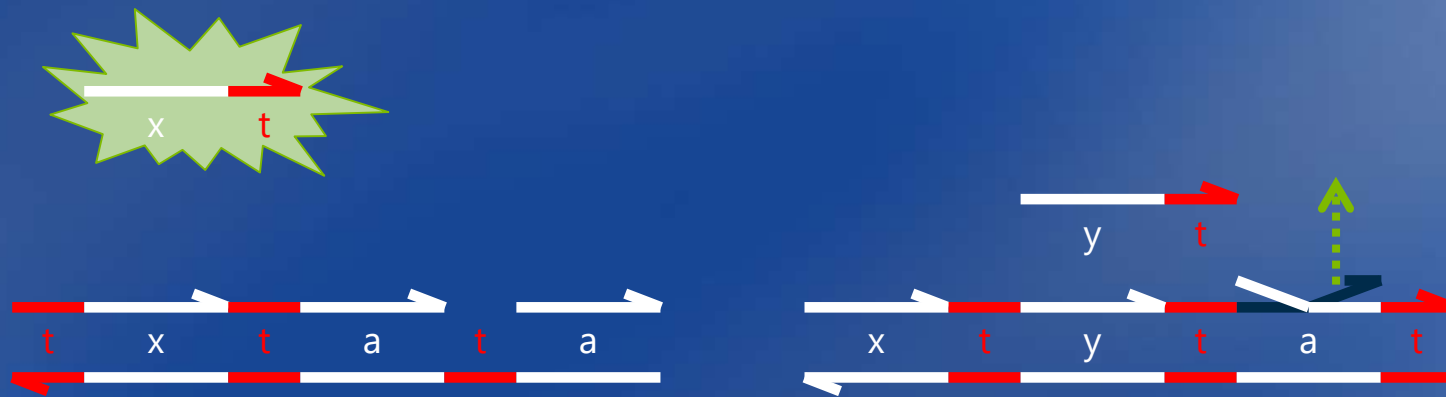


Transducer $x \rightarrow y$



So far, a **tx** signal has produced an **at** cosignal.
But we want signals as output, not cosignals.

Transducer $x \rightarrow y$



Transducer $x \rightarrow y$



Transducer $x \rightarrow y$



Transducer $x \rightarrow y$



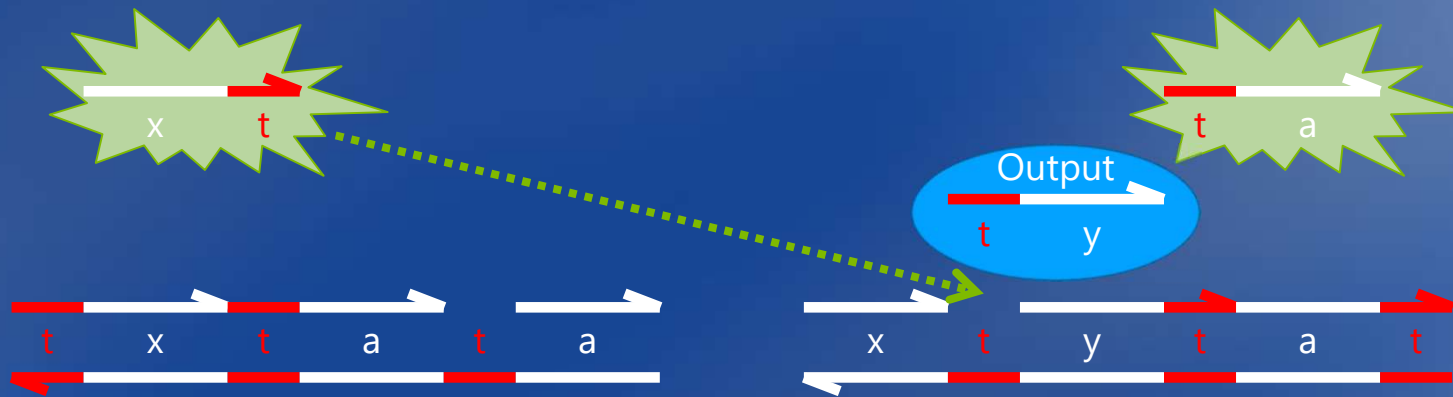
Here is our output **ty** signal.

But we are not done yet:

- 1) We need to make the output irreversible.
- 2) We need to remove the garbage.

We can use (2) to achieve (1).

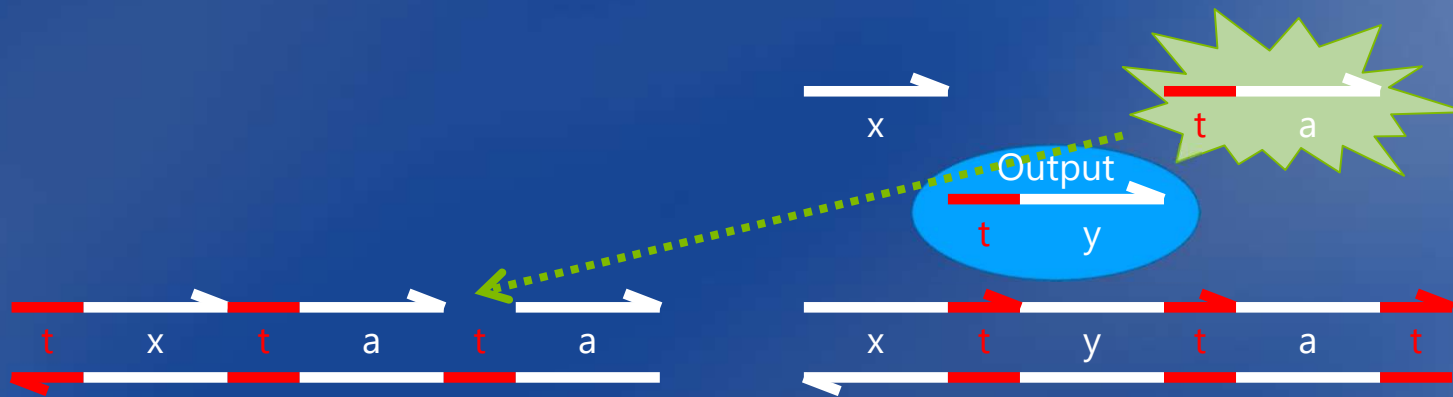
Transducer $x \rightarrow y$



Transducer $x \rightarrow y$



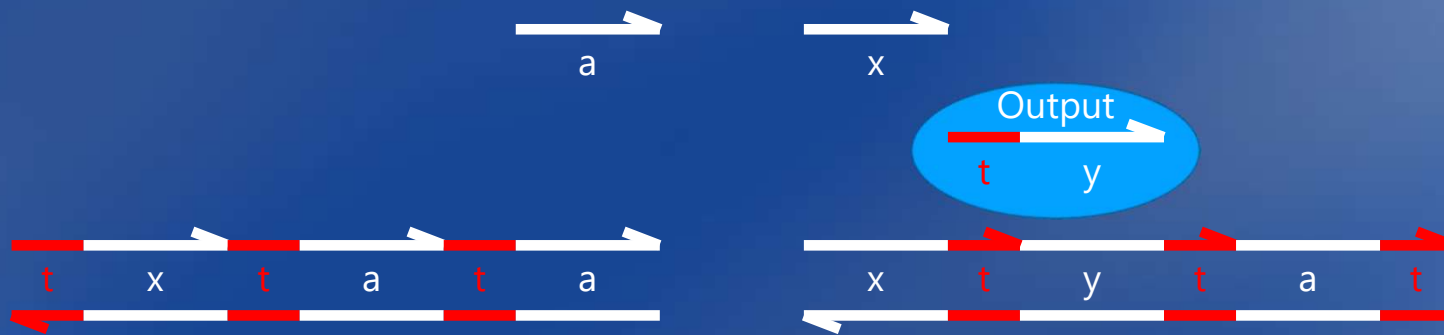
Transducer $x \rightarrow y$



Transducer $x \rightarrow y$



Transducer $x \rightarrow y$



Transducer $x \rightarrow y$

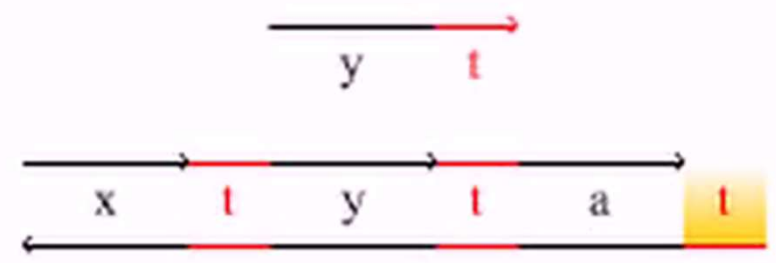
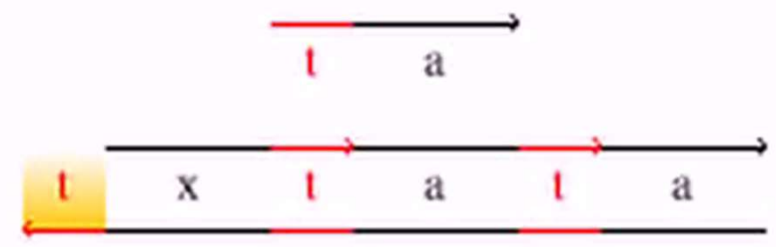


Done.

N.B. the gate is consumed: it is the energy source

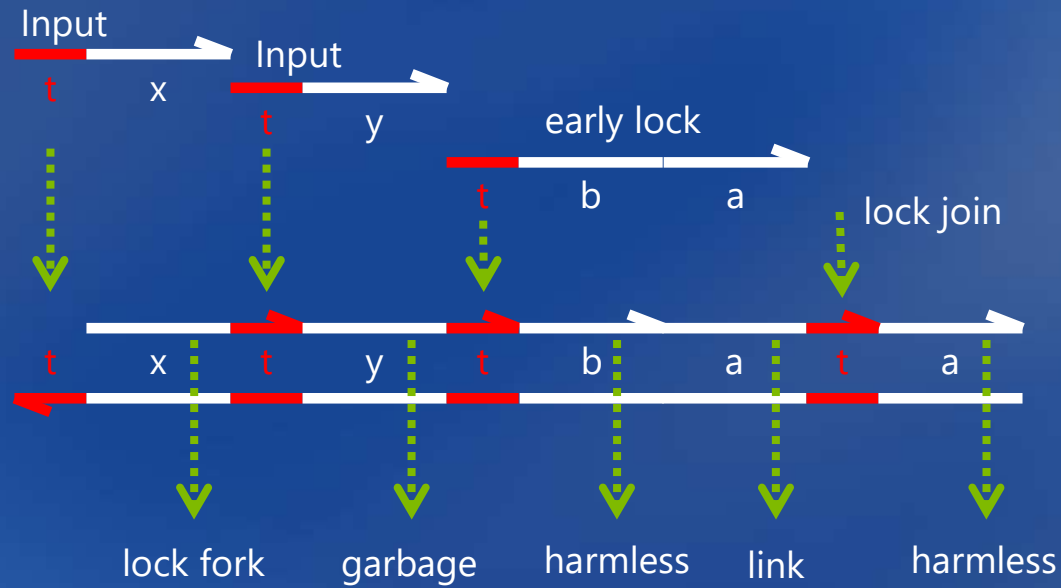
(no proteins, no enzymes, no heat-cycling, etc.; just DNA in salty water)

Transducer $x \rightarrow y$



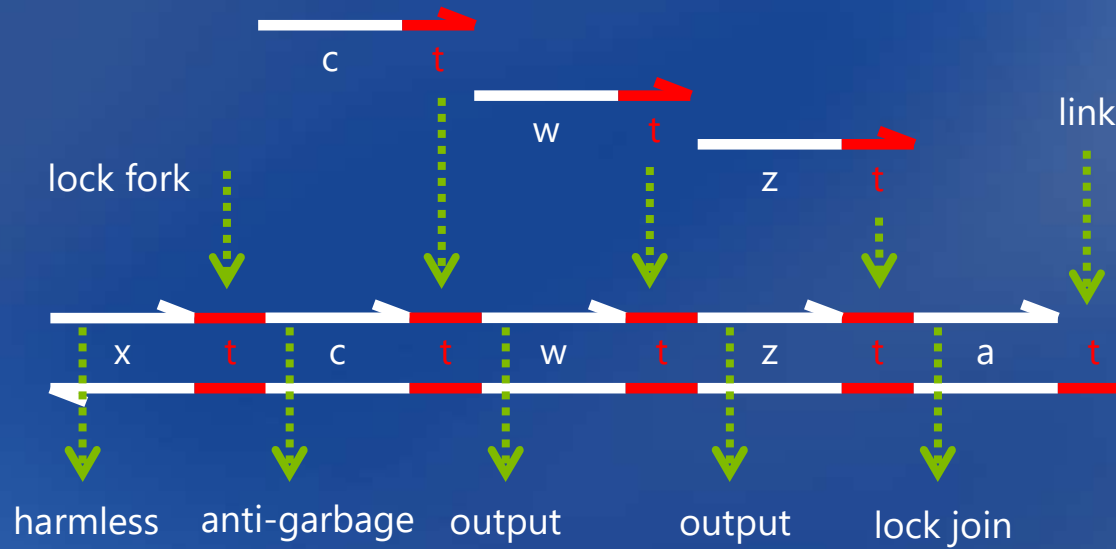
Reaction $x + y \rightarrow z + w$

join
half



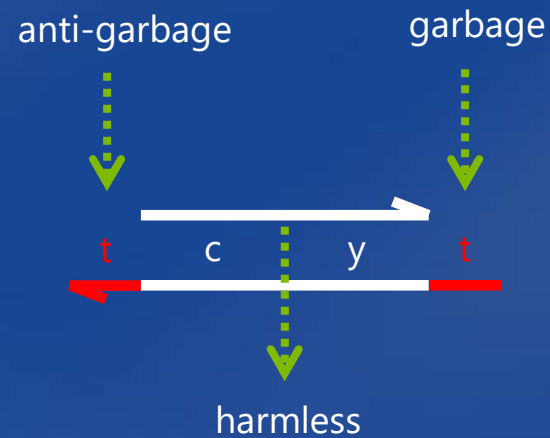
Reaction $x + y \rightarrow z + w$

fork
half



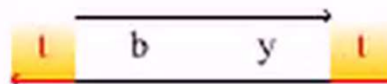
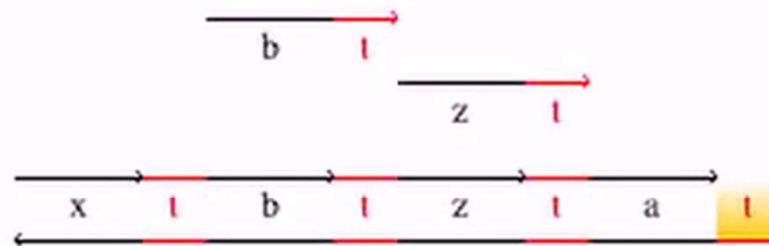
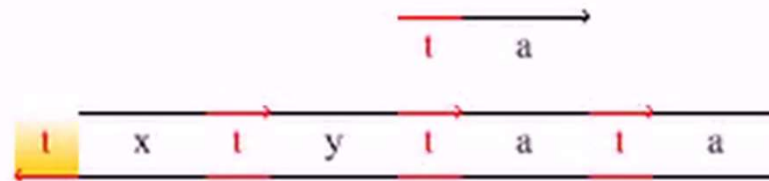


garbage
collection



Powered by Sothink

Join $x+y \rightarrow z$



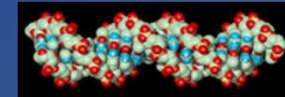
Approximate Majority Algorithm

- Given two populations of agents (or molecules)
 - Randomly communicating by radio (or by collisions)
 - Reach an agreement about which population is in majority
 - By converting all the minority to the majority[Angluin et al., Distributed Computing, 2007]

- 3 rules of agent (or molecule) interaction



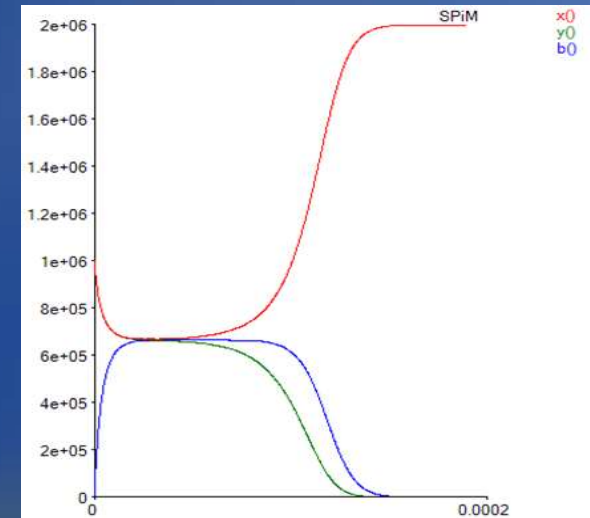
“our program”



Optimal Consensus Algorithm

- Fast: reaches agreement in $O(\log n)$ time w.h.p.
 - $O(n \log n)$ communications/collisions
 - Even when initially $\#X = \#Y!$ (stochastic symmetry breaking)
- Robust: true majority wins w.h.p.
 - If initial majority exceeds minority by $\omega(\sqrt{n \log n})$
 - Hence the agreement state is stable

Stochastic simulation of worst-case scenario with initially $\#X = \#Y$

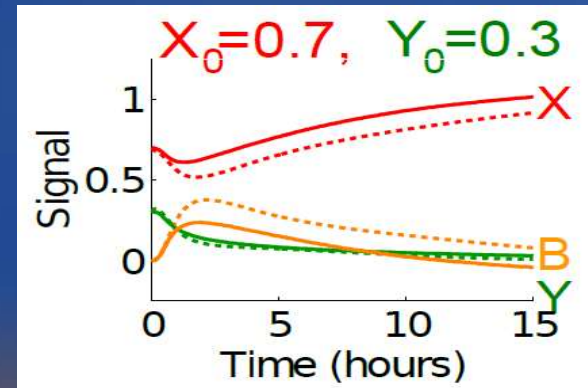
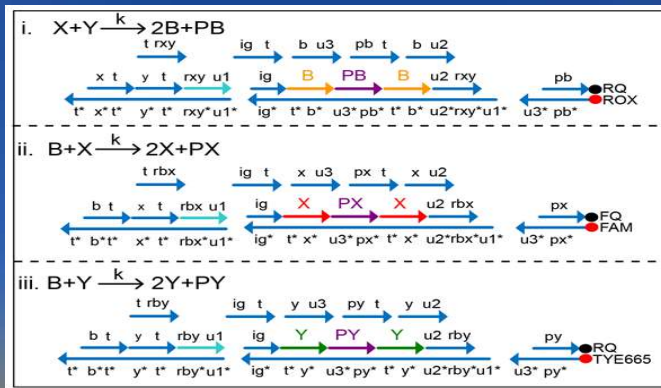


DNA Implementation of the Approximate Majority algorithm

nature
nanotechnology

Programmable chemical controllers made from DNA

Yuan-Jyue Chen, Neil Dalchau, Niranjan Srinivas, Andrew Phillips, Luca Cardelli, David Soloveichik & Georg Seelig

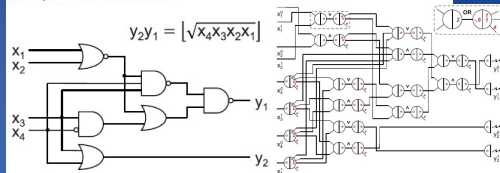


Some Large-scale Circuits (so far...)

3 JUNE 2011 VOL 332 SCIENCE

Scaling Up Digital Circuit Computation with DNA Strand Displacement Cascades

Lulu Qian¹ and Erik Winfree^{1,2,3*}

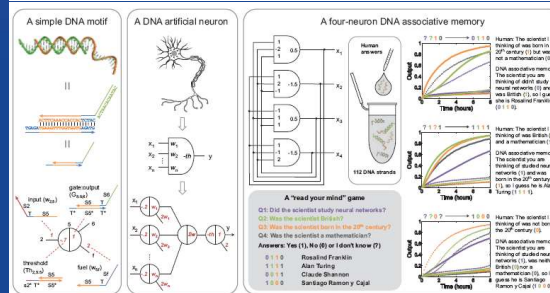


Computing the square root of a 4-bit number

368 | NATURE | VOL 475 | 21 JULY 2011

Neural network computation with DNA strand displacement cascades

Lulu Qian¹, Erik Winfree^{1,2,3} & Joshua Bruck^{3,4}

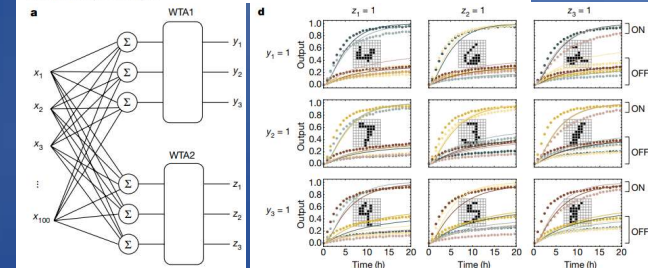


Classifying 4 distinct 4-bit patterns via 4 neurons

370 | NATURE | VOL 559 | 19 JULY 2018

Scaling up molecular pattern recognition with DNA-based winner-take-all neural networks

Kevin M. Cherry¹ & Lulu Qian^{1,2*}



Classifying 9 distinct 100-bit patterns via WTA networks

Scaling up: DNA Circuit Boards

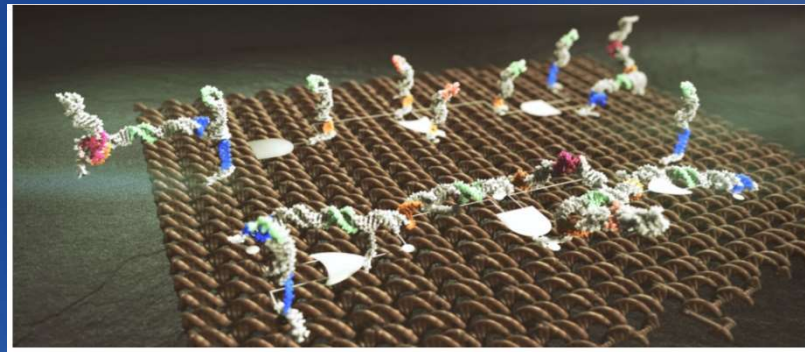
ARTICLES

PUBLISHED ONLINE: 24 JULY 2017 | DOI: 10.1038/NNANO.2017.127

nature
nanotechnology

A spatially localized architecture for fast and modular DNA computing

Gourab Chatterjee¹, Neil Dalchau², Richard A. Muscat³, Andrew Phillips^{2*} and Georg Seelig^{3,4*}

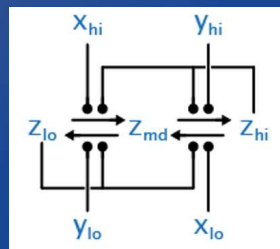
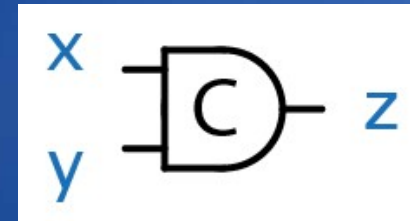


The first computational circuit boards made of DNA

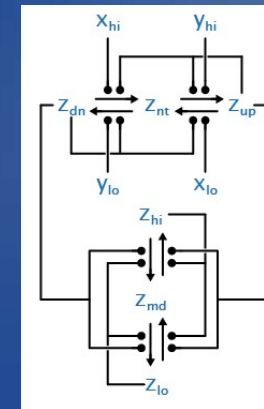
<https://www.microsoft.com/en-us/research/blog/researchers-build-nanoscale-computational-circuit-boards-dna>

Avoiding Clocks

- Muller C-Element
 - A Boolean gate
 - When $x = y$ then $z = x = y$, otherwise z remembers its *last* state.



Core C-Element
(AM with external inputs)



Full C-Element with output
rectified by another AM

Chemical Reaction Network Designs for Asynchronous Logic Circuits.

Luca Cardelli, Marta Kwiatkowska, Max Whitby.
Natural Computing Journal.

Algorithm Design

A software pipeline for Molecular Programming

Development Tools

MSRC Biological Computation Group

Visual DSD

A Development Environment for DNA Strand Displacement

The screenshot shows the Interface software interface. On the left, a code editor displays the following code:

```
def bind = kt*1.0e-9 (* /nM/s *)
def unbind = kt*exp_DeltaG_over_RT (* /s *)
new t@bind,unbind
new u@bind,unbind
new f1@0.0,0.0

def onex = 50.0

(* x + y -> y + z *)
def Cat(N,x,y,z) =
  new a
  ( (1.5*N) * t^x:[x t^y]:[y u^z]:[a]
  | (1.5*N) * [x]:[t^z]:[t^y]u^x
  | (2.0*N) * <u^ a>
  | (2.0*N) * <z t^>
  )

def Rep(N,x,f1) =
  ((3.0*N) * t^x:[x]<f1^>)

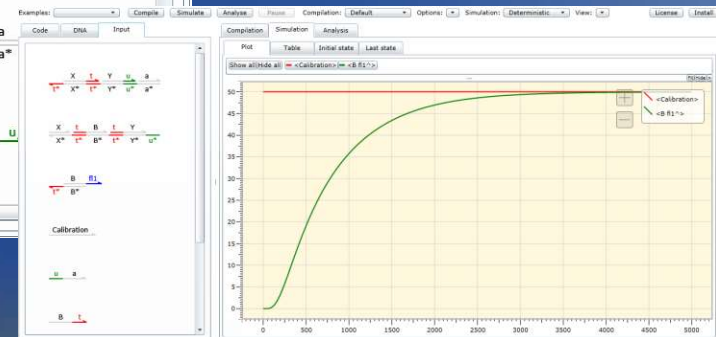
(onex = <Calibration>
| Cat(onex,X,Y,B)
| Rep(onex,B,f1)
| onex = <t^ X>
| onex = <t^ Y>
)
```

The central panel shows several reaction diagrams for DNA strand displacement. Each diagram consists of horizontal lines representing DNA strands with colored segments (red, green, blue) and arrows indicating the direction of displacement. Reactions are shown with double-headed arrows, indicating reversible processes.

JOURNAL OF THE ROYAL SOCIETY **Interface**

A programming language for composable DNA circuits

Andrew Phillips and Luca Cardelli

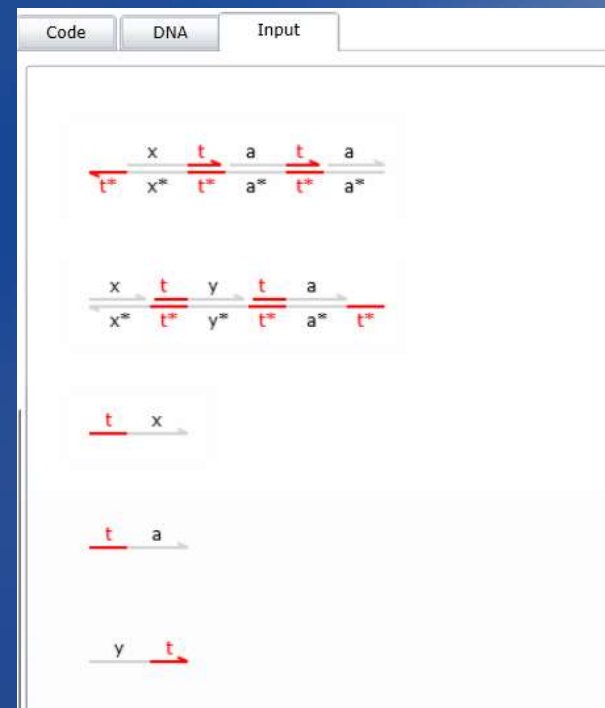


A Language for DNA Structures

- Describe the initial *structures* (not behavior)

```
Code DNA Input
directive duration 10000.0 points 1000
directive plot <t^ x>; <t^ y>; <t^ z>
new t
def T(N,x,y) =
  new a
  ( N * <t^ a>
  | N * <y t^>
  | N * t^*: [x t^]: [a t^]: [a] (* Input gate *)
  | N * [x]: [t^ y]: [t^ a]: t^* (* Output gate *)
  )
( <t^ x> | T(1,x,y) )
```

=



Compute Species and Reactions

- Recursively computed from the initial structures

Species

Reactions

Graph

Text

Domains

SBML

Compilation

Simulation

Analysis

Species

Reactions

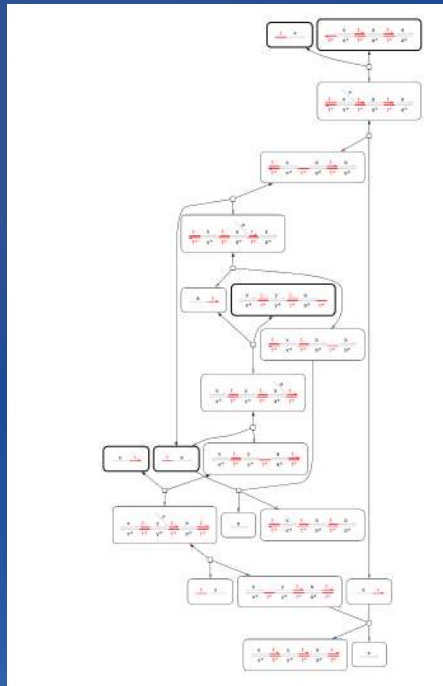
Graph

Text

Domains

SBML

Reaction Graph and Export



```
Compilation Simulation Analysis
Species Reactions Graph Text Domains SBML
Save as XML
<?xml version="1.0" encoding="UTF-8"?>
<sbml xmlns="http://www.sbml.org/sbml/level2/version1" level="2" version="1">
<model>
<listOfCompartments>
<compartment id="c" size="1"/>
</listOfCompartments>
<listOfSpecies>
<species id="s_id0" name="&t^ x^" compartment="c" initialAmount="1" constant="false"/>
<species id="s_id1" name="&t^ a^" compartment="c" initialAmount="1" constant="false"/>
<species id="s_id2" name="&t^ y^" compartment="c" initialAmount="1" constant="false"/>
<species id="s_id3" name="[t^*][x t^]:[a t^]:[a]" compartment="c" initialAmount="1" constant="false"/>
<species id="s_id4" name="[t^ x]:&t;x>:[t^]:[a t^]:[a]" compartment="c" initialAmount="0" constant="false"/>
<species id="s_id5" name="[t^ x]{t^*}:[a t^]:[a]" compartment="c" initialAmount="0" constant="false"/>
<species id="s_id6" name="[t^ x]:[t^ a]:&t;a>:[t^]:[a]" compartment="c" initialAmount="0" constant="false"/>
<species id="s_id7" name="[t^ x]:[t^ a]{t^*}:[a]" compartment="c" initialAmount="0" constant="false"/>
<species id="s_id8" name="[t^ x]:[t^ a]:[t^ a]" compartment="c" initialAmount="0" constant="false"/>
<species id="s_id9" name="&t;a^" compartment="c" initialAmount="0" constant="false"/>
<species id="s_id10" name="&t;a t^" compartment="c" initialAmount="0" constant="false"/>
<species id="s_id11" name="&t;x t^" compartment="c" initialAmount="0" constant="false"/>
<species id="s_id12" name="[x]:[t^ y]:[t^ a]{t^*}" compartment="c" initialAmount="1" constant="false"/>
<species id="s_id13" name="[x]:[t^ y]:[t^ a]:&t;a>:[t^]" compartment="c" initialAmount="0" constant="false"/>
<species id="s_id14" name="[x]:[t^ y]{t^*}:[a t^]" compartment="c" initialAmount="0" constant="false"/>
<species id="s_id15" name="[x]:[t^ y]:&t;y>:[t^]:[a t^]" compartment="c" initialAmount="0" constant="false"/>
<species id="s_id16" name="[x]{t^*}:[y t^]:[a t^]" compartment="c" initialAmount="0" constant="false"/>
<species id="s_id17" name="[x t^]:[y t^]:[a t^]" compartment="c" initialAmount="0" constant="false"/>
<species id="s_id18" name="&t;x^" compartment="c" initialAmount="0" constant="false"/>
<species id="s_id19" name="&t;y^" compartment="c" initialAmount="0" constant="false"/>
</listOfSpecies>
<listOfReactions>
<reaction id="r_id20" reversible="false">
<listOfReactants>
<speciesReference species="s_id3"/>
<speciesReference species="s_id0"/>
```

Simulation

- Deterministic
- Stochastic (Gillespie)
- Probabilistic (CME)
- Linear Noise Approximation
- "JIT"



State Space Analysis

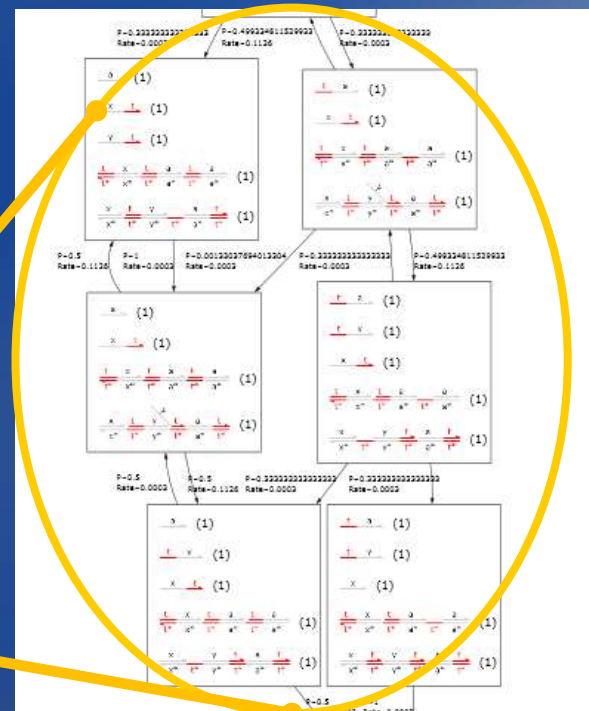
Compilation Simulation Analysis
Graph Text PRISM Visualise

INITIAL STATE:

- $\frac{t}{x^m} a (1)$
- $\frac{t}{x^m} x (1)$
- $y \frac{t}{x^m} (1)$
- $\frac{x}{x^m} \frac{t}{t^m} \frac{y}{y^m} \frac{t}{t^m} \frac{a}{a^m} (1)$
- $\frac{x}{t^m} \frac{t}{x^m} \frac{a}{t^m} \frac{t}{a^m} (1)$

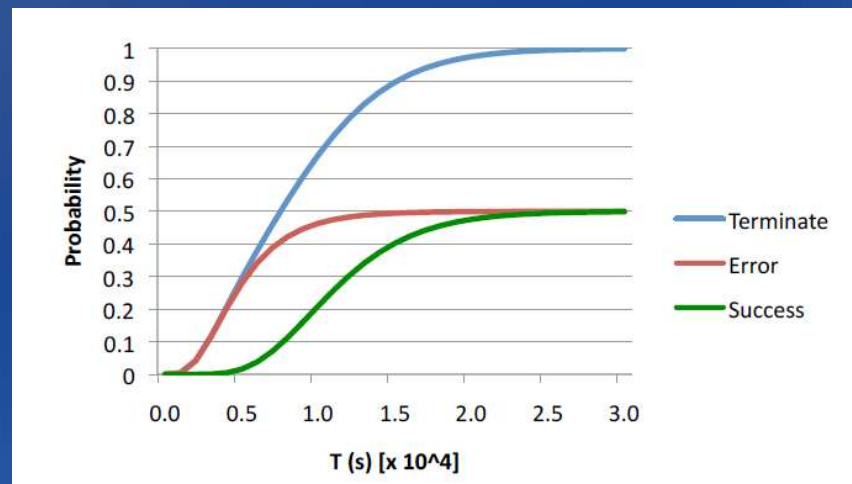
TERMINAL STATE:

- $a (1)$
- $\frac{t}{x^m} y (1)$
- $x (1)$
- $\frac{t}{t^m} \frac{x}{x^m} \frac{t}{t^m} \frac{a}{a^m} \frac{t}{t^m} \frac{a}{a^m} (1)$
- $\frac{x}{x^m} \frac{t}{t^m} \frac{y}{y^m} \frac{t}{t^m} \frac{a}{a^m} \frac{t}{t^m} (1)$



Modelchecking

- Export to PRISM probabilistic modelchecker



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OF
THE ROYAL
SOCIETY

Interface

Design and analysis of DNA strand displacement devices using probabilistic model checking

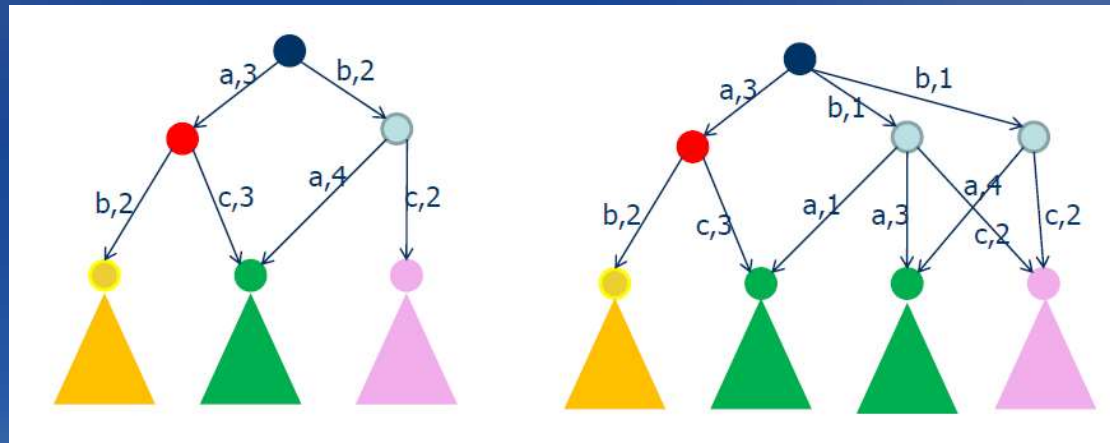
Matthew R. Lakin^{1,3,†}, David Parker^{2,†}, Luca Cardelli¹,
Marta Kwiatkowska² and Andrew Phillips^{1,*}

Verification

- Quantitative theories of system equivalence and approximation.

CONTINUOUS MARKOVIAN LOGICS
AXIOMATIZATION AND QUANTIFIED METATHEORY

RADU MARDARE, LUCA CARDELLI, AND KIM G. LARSEN



Physical Execution

A wetlab pipeline for Molecular Programming

Computer Aided Design

MSRC Biological Computation Group

Visual DSD

A Development Environment for DNA Strand Displacement

The screenshot shows the Interface software interface. On the left, a code editor displays the following code:

```
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def unbind = kt*exp_DeltaG_over_RT (* /s *)
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new u@bind,unbind
new f1@0.0,0.0

def onex = 50.0

(* x + y -> y + z *)
def Cat(N,x,y,z) =
  new a
  ( (1.5*N) * t^x:[x t^y]:[y u^z]:[a]
  | (1.5*N) * [x]:[t^x z]:[t^y y]:u^z
  | (2.0*N) * <u^ a>
  | (2.0*N) * <z t^>
  )

def Rep(N,x,f1) =
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(onex = <Calibration>
| Cat(onex,X,Y,B)
| Rep(onex,B,f1)
| onex = <t^ X>
| onex = <t^ Y>
)
```

The central panel displays several visual diagrams of DNA strand displacement reactions. Each diagram shows a set of DNA strands (represented by lines with colored segments) and their interactions, with arrows indicating the direction of the reaction. The diagrams are arranged in a grid, showing different stages and types of reactions.

JOURNAL OF THE ROYAL SOCIETY

Interface

A programming language for composable DNA circuits

Andrew Phillips and Luca Cardelli

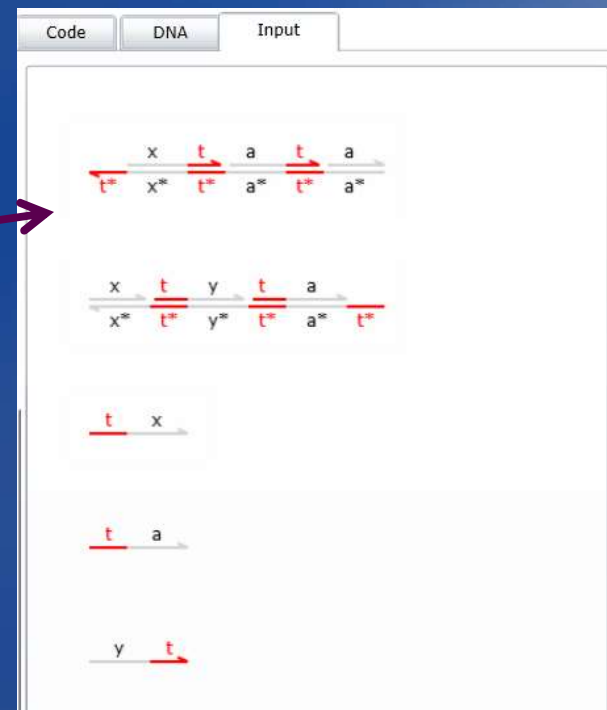


Output of Design Process

- Domain structures
 - (DNA sequences to be determined)

“Ok, how do I run this for real?”

“What are the actual DNA sequences?”

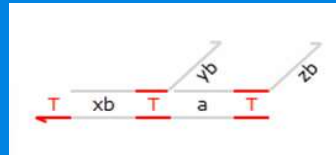


From Structures to Sequences



www.nupack.org

DSD Structure → "Dot-Paren" representation



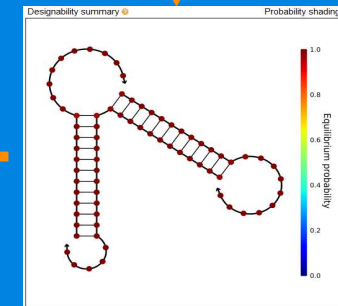
Nucleic acid type: RNA DNA Temperature: °C Number of designs:

Target structure:

Output Sequences

Ensemble defect (nt)	Normalized ensemble defect (%)	GC content (%)	Sequence
0.2	0.3	57.5	GCUGCGAUACCCAAAAGAAC AA+GCGAUCAAGCCCCUCU UUUCC+GGGCUUGAUCGCGG GUAUCGACGUCGCGC

Thermodynamic Synthesis



"Ok, where do I buy these?"



"DNA Synthesis"

dna synthesis × Search

About 8,610,000 results (0.24 seconds) Advanced search

► **Custom DNA Synthesis** Ads
www.Biomatik.com High Quality Custom Gene **Synthesis**, Best Price Guaranteed! Get A Quote.

Order Gene at GenScript
www.GenScript.com \$0.29/bp. Any Gene in ANY Vector Proven increase protein expression

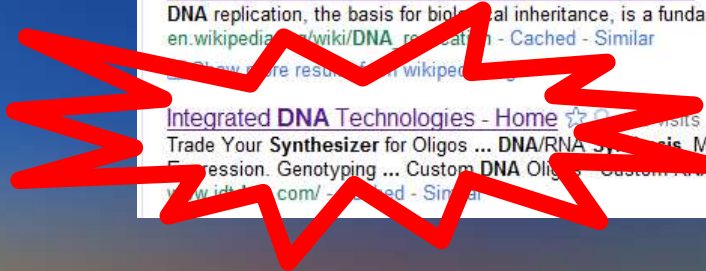
Gene Synthesis \$0.35/bp
www.epochlifescience.com Dependable Service @ Low Price: Come on Down and Save Your Budgets!

DNA synthesis - Wikipedia, the free encyclopedia ☆ 🔍
DNA **synthesis** commonly refers to: DNA replication - DNA biosynthesis (in vivo DNA amplification); Polymerase chain reaction - enzymatic **DNA synthesis** (in ...
en.wikipedia.org/wiki/DNA_synthesis - Cached - Similar

DNA replication - Wikipedia, the free encyclopedia ☆ 🔍
DNA replication, the basis for biological inheritance, is a fundamental ...
en.wikipedia.org/wiki/DNA_replication - Cached - Similar

Show more results from wikipedia

Integrated DNA Technologies - Home ☆ 🔍 Visits - May 24
Trade Your **Synthesizer** for Oligos ... **DNA/RNA Synthesis**. Modifications. Purifications. Gene Expression. Genotyping ... Custom **DNA Oligos** ... Custom **DNA Oligos** ...
www.idt.com/ - Cached - Similar



From Sequences to Molecules

- Copy&Paste from nupack

XX-IDT
INTEGRATED DNA TECHNOLOGIES

Chat is now closed. Please click to email a representative. 

[LogIn] Spain

0 Items € 0,00

Home Products Order Support Services SciTools Search Go

Order Oligos

Change Form: 1 Expand to this many items Duplex Paste Go

25 nmole DNA Oligo = 15-60 bases 100 nmole DNA oligo = 10-90 bases 250 nmole DNA oligo = 5-100 bases
1 μmole DNA oligo = 5-100 bases 5 μmole DNA oligo = 5-50 bases 10 μmole DNA oligo = 5-50 bases
25 nmole Ultramer DNA Oligo = 60-200 bases 4 nmole Ultramer DNA Oligo = 60-200 bases PAGE Ultramer DNA Oligo = 60-200 bases

Scale: 25 nmole DNA oligo Purification: Standard

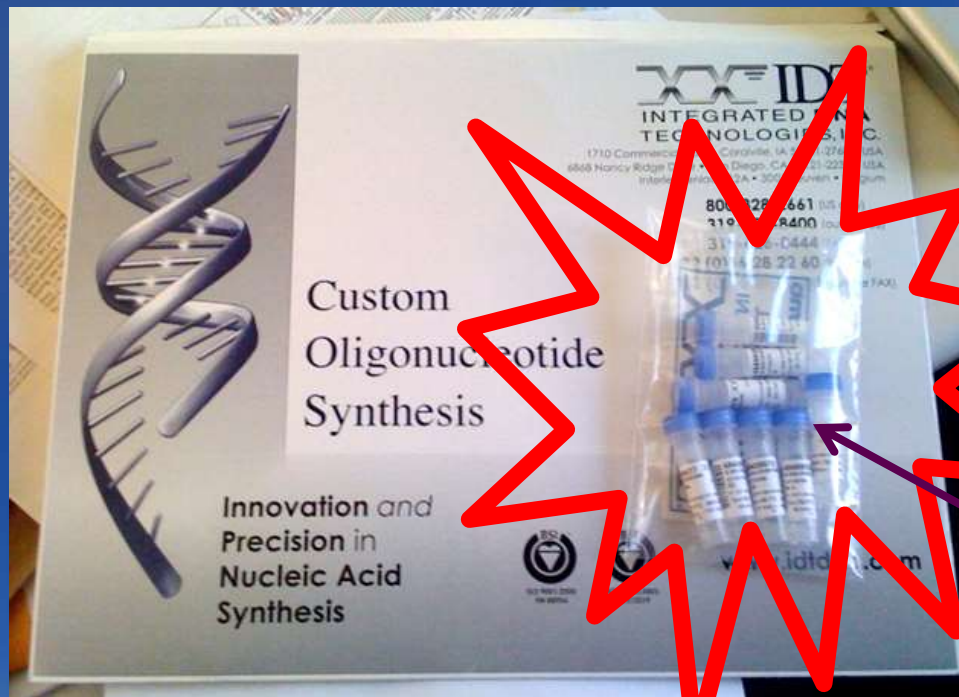
Sequence Name: 5'-ACT GCA CCA TAA GCA ACT TTT

ADD TO ORDER
ADD TO WISH LIST

Preparative Services
 LabReady (more detail) € 2,82 EUR

Customized Labels (more detail)
Stock IDT Label FREE

Molecules by FedEx



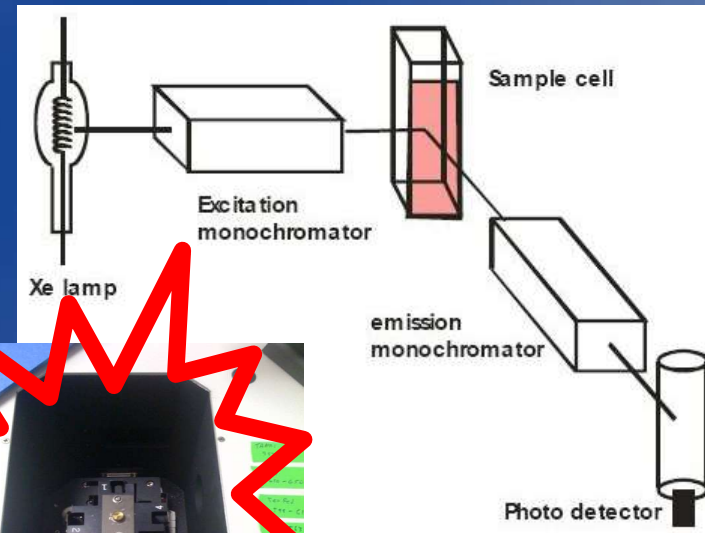
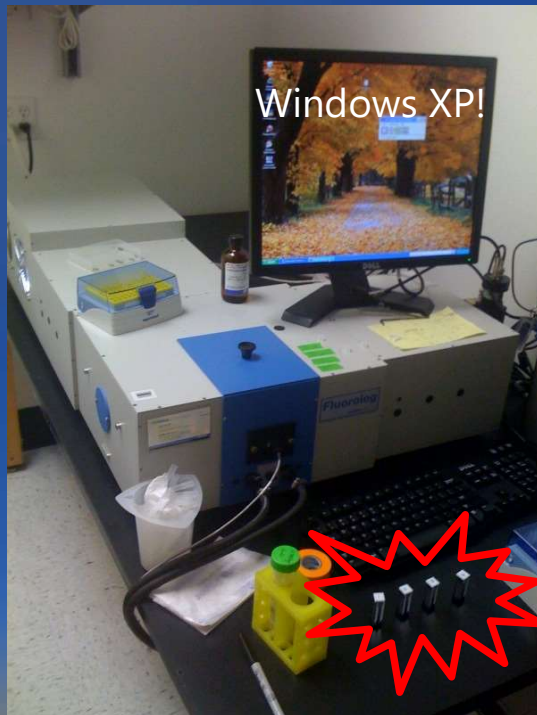
"Ok, how do I run these?"

Add Water

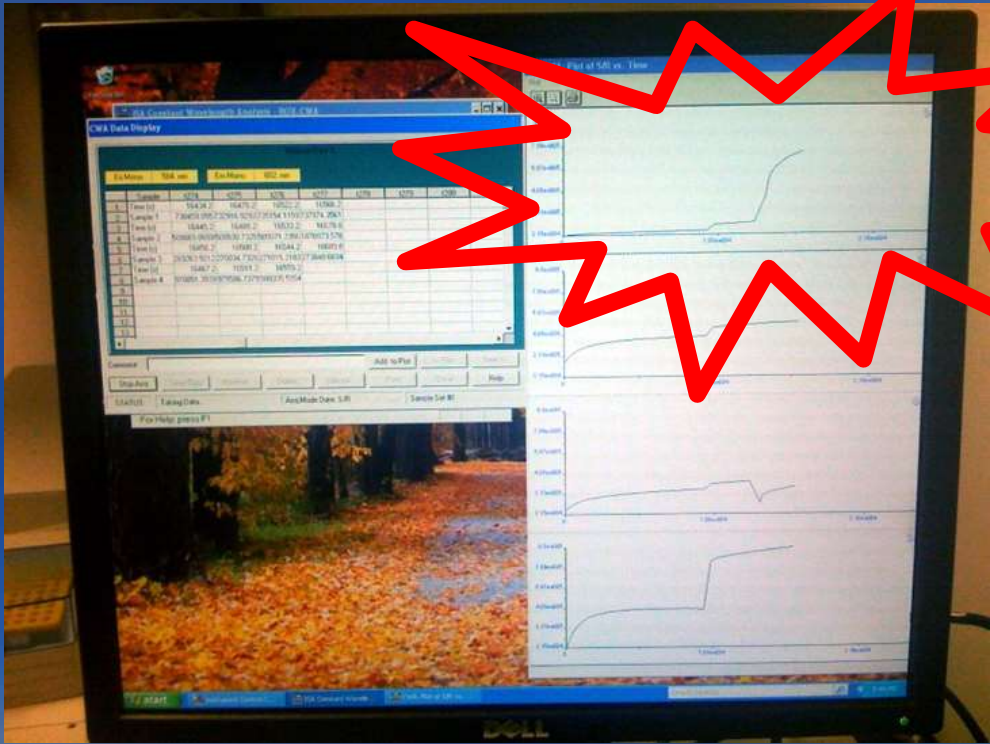


Execute (finally!)

- Fluorescence is your one-bit 'print' statement



Output

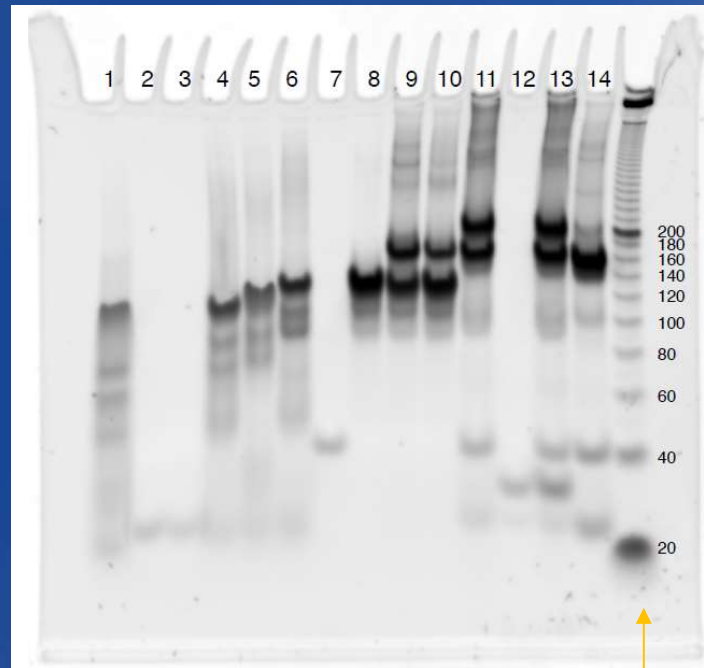


Debugging

- A core dump

DNA strand length

polyacrylamide gel electrophoresis



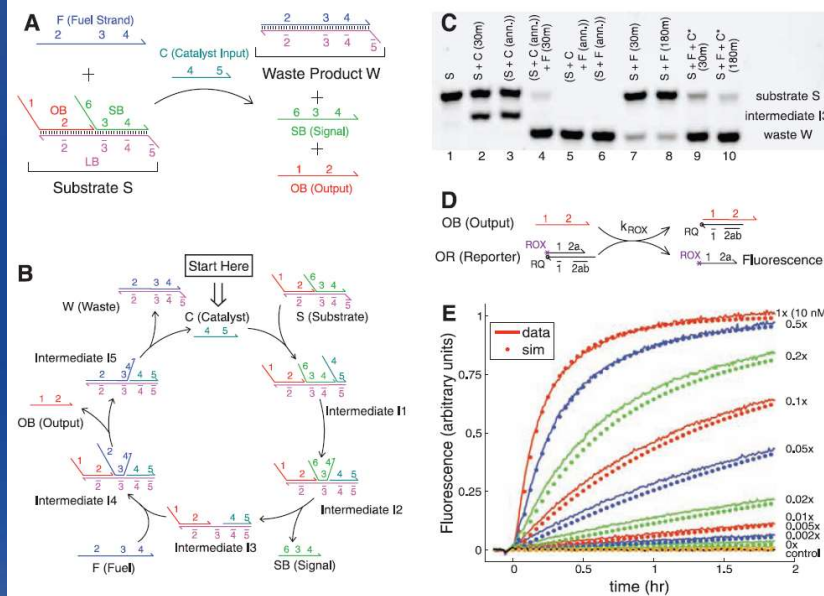
Various processing stages

Calibration scale

Delivery!

Engineering Entropy-Driven Reactions and Networks Catalyzed by DNA

David Yu Zhang, *et al.*
Science **318**, 1121 (2007);
 DOI: 10.1126/science.1148532



Final Remarks

"Modern" DNA Computing

- Non-goals
 - Not to solve NP-complete problems with large vats of DNA
 - Not to replace silicon
- Bootstrapping a carbon-based technology
 - To precisely control the organization and dynamics of matter and information at the molecular level
 - DNA is our engineering material
 - Its biological origin is "accidental" (but convenient)
 - It is an information-bearing programmable material
 - Other such materials will be (are being) developed

State of the art

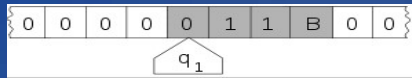
- Building a full software/hardware pipeline for a new fundamental technology
 - Mathematical Foundations [~ concurrency theory in the 80's]
 - Programming Languages [~ software engineering in the 70's]
 - Analytical Methods and Tools [~ formal methods in the 90's]
 - Device Architecture and Manufacturing [~ electronics in the 60's]
- To realize the potential of Molecular Programming
- “With *no alien technology*” [David Soloveichik]
- We have some good strategies. Device design is now largely a ‘software problem’ but with a significant ‘engineering scaleup and integration’ problem

Ongoing Challenges

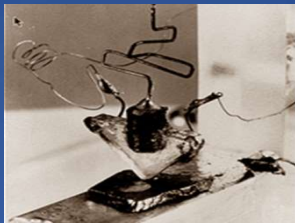
- In-vivo DNA survivability
- Complexity (and crosstalk)
- Manufacturing
- Speed
- Energy

A Brief History of DNA

Turing Machine, 1936



Transistor, 1947



Computer programming

20th century

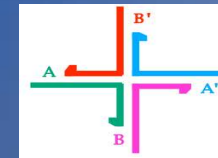
DNA, -3,800,000,000



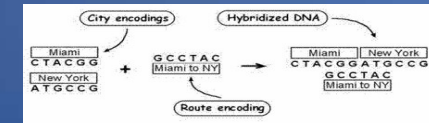
Systematic manipulation of information

Systematic manipulation of matter

Structural DNA Nanotech, 1982



DNA Algorithm, 1994



Molecular programming

21th century

Resources

- DNA Computing and Molecular Programming Conference - incarnations since 1995

<http://www.dna-computing.org/>

- Molecular Programming Project (Caltech - U.W. - Harvard - UCSF)
<http://molecular-programming.org/> (2008-2018 NSF Expeditions in Computing)

- Georg Seelig's DNA Nanotech Lab at U.W. CS&E
<http://homes.cs.washington.edu/~seelig/>

- Biological Computation Group at Microsoft
<https://www.microsoft.com/en-us/research/group/biological-computation/>